

DES CARTES. This famous French philosopher and mathematician wrote when he was very young, and indeed while he was engaged in the profession of a foldier and lay in garrison at Breda, a treatise called *Musicae Compendium*; which was published in the year 1617; and comprehends the following articles. 'De numero vel tempore in sonis observando. De sonorum diversitate circa acutum et grave. De consonantiis. De octavâ. De quintâ. De quartâ. De ditono, tertiâ minore, et sextis. De gradibus five tonis musicis. De dissonantiis. De ratione componendi et modis. De modis.'

This Compendium of Music, though it is comprized in fifty-eight small quarto pages, contains a great number of very curious particulars relative to the science. The observations of Des Cartes on the effects of various measures are new and judicious.

'We say in the generall that a slow measure doth excite in us gentle and sluggish motions, such as a kind of languor, sadness, fear, pride, and other heavy and dull passions: and a more nimble and swift measure doth proportionably excite more nimble and sprightly passions; such as joy, anger, courage, &c. the same may also be sayd of the double kind of percussion, viz. that a quadrate, or such as is perpetually resolved into equals, is slower and duller than a tertiate, or such as doth consist of three equal parts. The reason whereof is, because this doth more possess and employ the sense, inasmuch as therein are more, namely 3, members to be adverted, while in the other are only 2.'

In his enumeration of the consonances, contrary to the sense of all other writers, from John De Muris to Merfennus, he excludes the unison; and for this very good reason, that 'therein is no difference of sounds as to acute and grave; it bearing the same relation to consonances, as unity doth to numbers.'

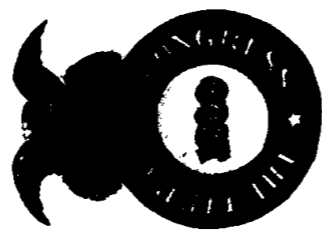
Of the two methods by which the diapason or octave is divided, the arithmetical and geometrical, Des Cartes, for the reasons contained in the sixth of his *Prænotanda*, prefers the former; and, for the purpose of adjusting the consonances, he proposes the division of a chord, first into two equal parts, and afterwards into smaller proportions, according to the following plan.

$\frac{1}{2}$	Eighth								
$\frac{1}{3}$	Twelfth	$\frac{2}{3}$	Fifth						
$\frac{1}{4}$	Fifteenth	$\frac{2}{4}$	Eighth	$\frac{3}{4}$	Fourth				
$\frac{1}{5}$	Seventeenth	$\frac{2}{5}$	Tenth Major	$\frac{3}{5}$	Sixth Major	$\frac{4}{5}$	Ditone		
$\frac{1}{6}$	Nineteenth	$\frac{2}{6}$	Twelfth	$\frac{3}{6}$	Eighth	$\frac{4}{6}$	Fifth	$\frac{5}{6}$	Third Minor

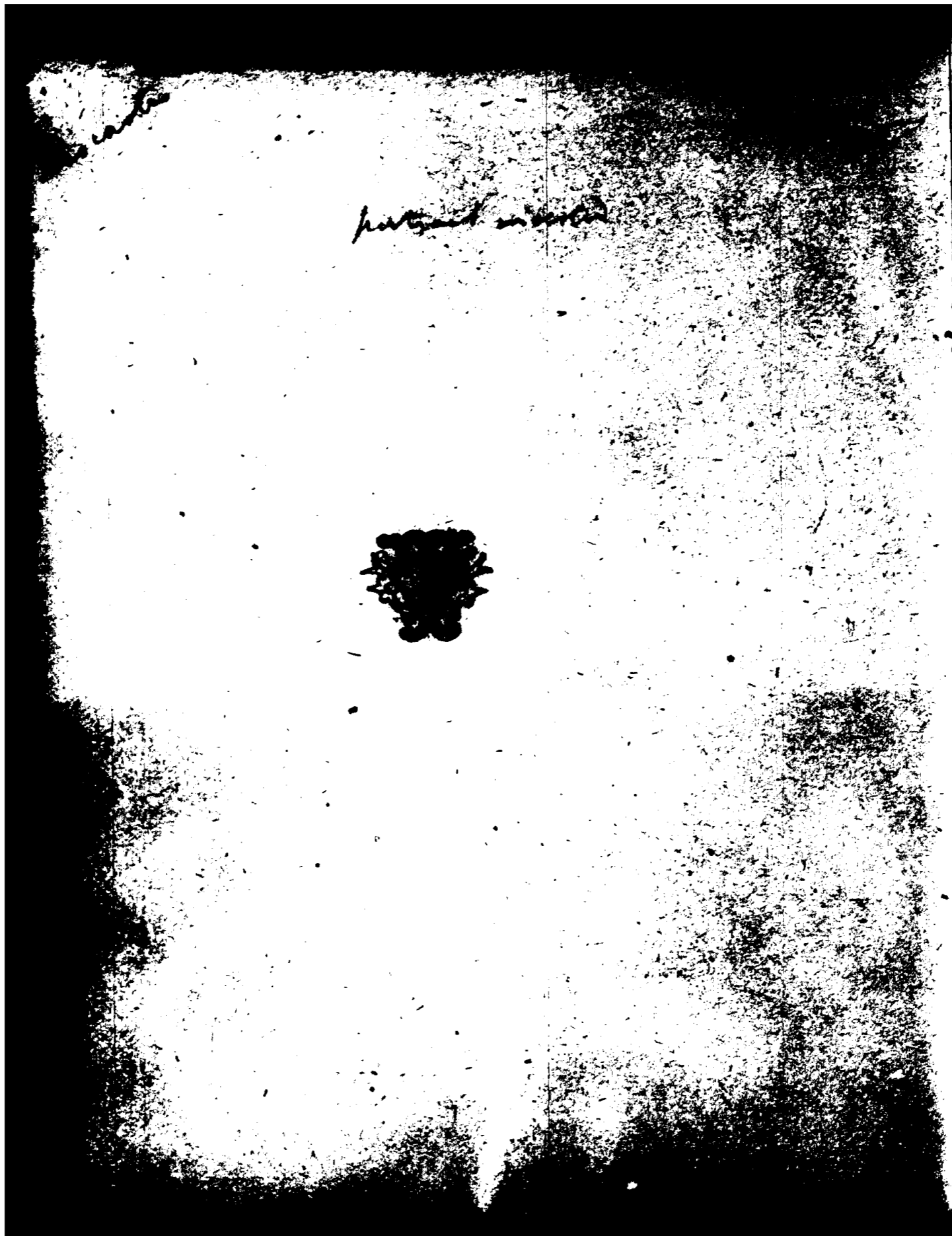
The advantages resulting from the geometrical division appear in the *Systema Participato*, mentioned by Bontempi, which consisted in the division of the diapason or octave into twelve equal semitones by eleven mean proportionals; Des Cartes, however, rejects this division, though his reasons for so doing are very far from satisfactory.

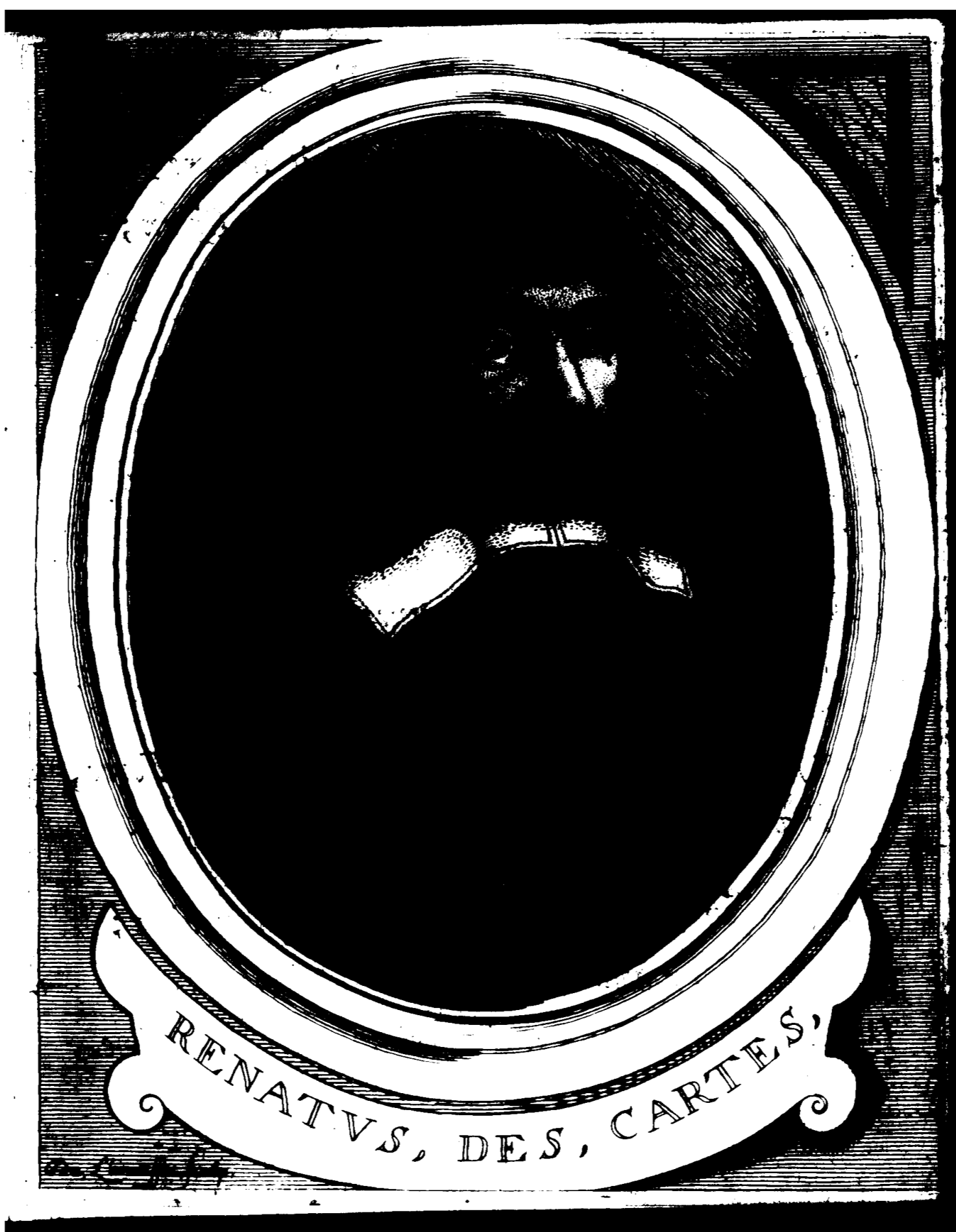
This book was translated into English in 1653, and published by a Person of Honour, (viz. William Lord Brouncker, president of the Royal Society, and the first appointed to that office;) with such animadversions as plainly shew that his lordship was deeply skilled in the theory of the science; but, though he almost everywhere agrees with his author, he scruples not to assert, that the geometrical is preferable to the arithmetical division; and, as it seems, with a view to a farther improvement of the *Systema Participato*, he proposes a division of the diapason by sixteen mean proportionals into seventeen equal semitones; the method of which division he exhibits in an algebraic process, as well as in logarithms. Notwithstanding the undoubted merit of this *Compendium of Descartes*, it contains some unaccountable singularities; of which the following extract may serve as a specimen.

' This only thing seems to render the voice of man the most grateful of all other sounds, that it holds the greatest conformity to our spirits. Thus also is the voice of a friend more grateful than that of an enemy, from a sympathy and dispathy of affections: by the same reason perhaps that it is conceived that a drum headed with a sheep's skin yields no sound though stricken, if another drum headed with a wolf's skin be beaten upon in the same room.'



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S O N N E T.

*Pour un Esprit si pur la Terre estoit impure ;
Cét Homme tout celeste est monté dans les Cieux ;
Il y void clairement ces flambeaux radieux ,
Dont nous n'avons icy qu'une lumiere obscure.*

*De ces voutes d'azur la noble Architecture
Ravit également son esprit & ses yeux ;
Et l'élevant plus haut que sa propre nature ,
Luy fait connoistre enfin la nature des Dieux.*

*Il me semble desja qu'au travers de ce verre ,
Dont son art approchoit le Ciel , l'Onde , & la Terre ,
Je le vois éclater au front du Firmament :*

*Et si l'on se transforme en la chose qu'on aime ;
Comme il fut amoureux des Astres seulement ,
Que le grand GALILÉE est un Astre luy-mesme.*

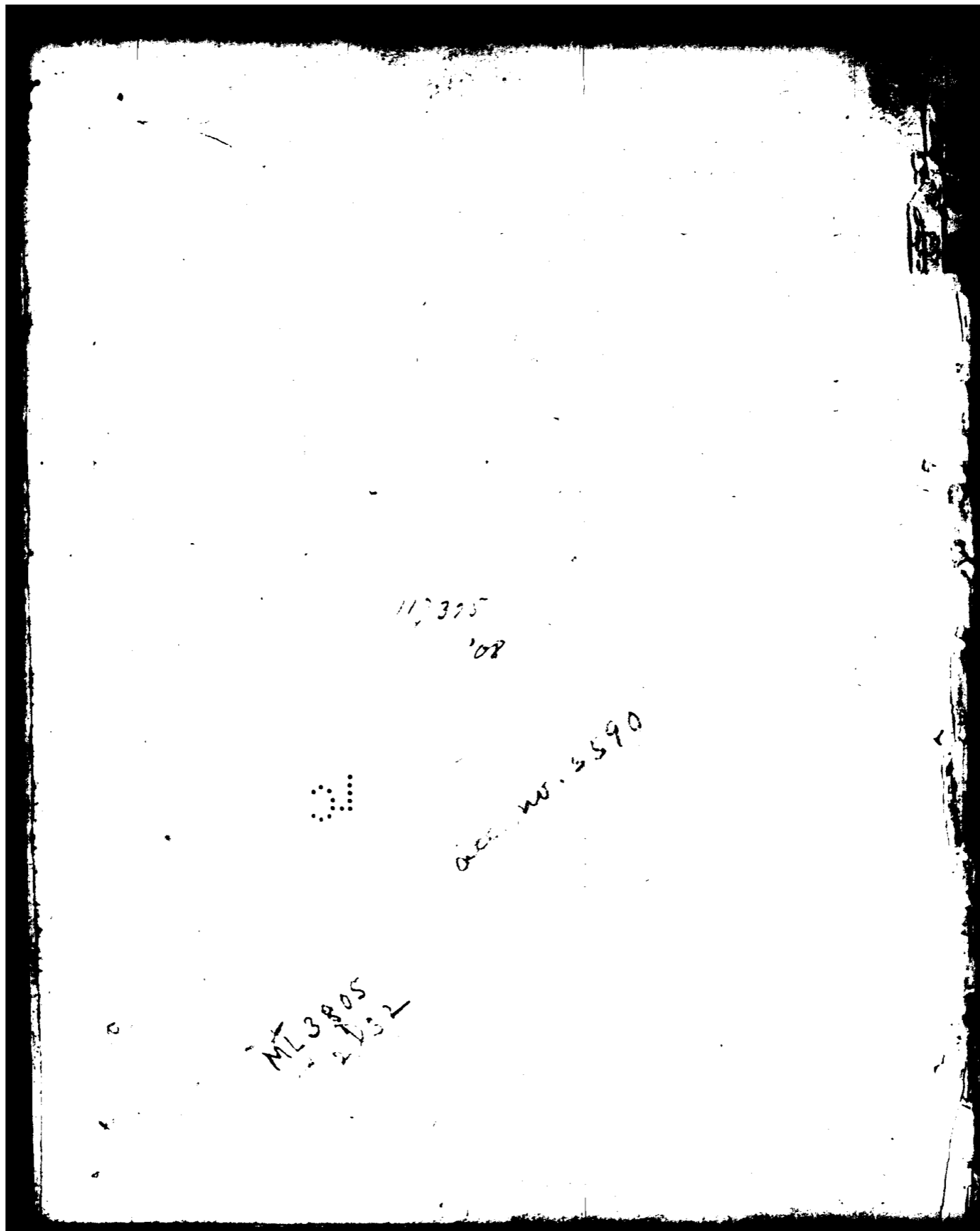
COLLETET.

RENATUS DESCARTES
EXCELLENT
COMPENDIUM
O F
MUSICK:
WITH
Necessary and Judicious
ANIMADVERSIONS
Thereupon.

By a Person of HONOUR.



*London, Printed by Thomas Harper, for Humphrey Moseley,
and are to be sold at his Shop at the Signe of the
Princes Armes in S. Pauls Church-Yard, and
by Thomas Heath in Coven Garden. 1653. 2.6x*



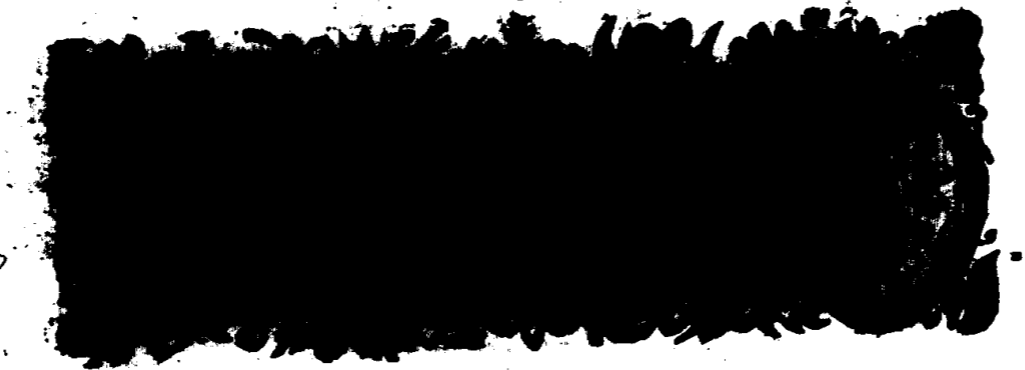
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THE
STATIONER
To the Ingenious
READER,
Or.

SIR:



*Sooner can your Eye have
taken in the Title of this
thin Volume, which I have,
in some latitude of Assistance,
Midwiv'd into this our
English World; but you shall most willing-
ly*

The Stationer

ly confesse it to be as well a sufficient Justification to my Industry and Cost, as a full Elogie to it selfe: The AUTHOR thereof, being one of the fairest Flowers in that Garland of the Mathematicks, wherewith this Century being meritoriously adorned, may, without breach of Modesty, take the right hand of Antiquity, and stand as well the Wonder, as Envy of Posterity: and so gratefully acknowledged by all, whose Studies and Ingenuity have qualified them with Judgement enough to profound the sense of his Geometry and Algebra. And its SUBJECT so universally Gratefull; that I dare say, you have not, in all your Readings, met with the Name of any Person, except onely Tacitus the Emperour, who was so rude and harsh of Disposition, as to dislike the Melody of Numbers.

Concerning the AUTHOR, therefore,
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to the Reader.

the most your selfe can judge me fit to say, is only this; that the most becoming Tribute I can pay unto his Noble Memory, is a silent Veneration: it being almost of Necessity, that a Panegyrick on Him from my unequal Pen, be interpreted a kind of implicite Diminution; since it must suppose the Height of His Merit to be commensurable by the Digits of so slender a Capacity; and few will admit Him for a Competent Doxologist, who is, by incomputable distances, below a due Apprehension of the Excellences of his Subject.

And, as for the SUBJECT likewise, wherewith the Rationall Soule of Man is so Pathetically, and by a kinde of occult Magnetisme, Affected, that even the most Rigid and Barbarous have ever Confest it to be the most potent Charme either to Excite, or Compose the most vehement Passi-

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ous thereof; as Homer ingeniously intimates in his *Figment*, that it was the Custom of the Gods, to pacifie their Civil Dissentions with the Harmony of Musick, and that the Rough spirited Achilles, with the soft Concordant Echoes of his owne Harp, used to Calme the tumultuous aestuation of his Choler; and as all Poets unanimously intend, in that they have made the Magick of Sirens to consist only in the sweet Accents and Melotheticall Modulation of their Voices: Concerning this, I say, it would sound a mere Pleonasm for me, here, to Commend it by any other Argument, but this unfrequent one. That the Sage and Upright Ancients had Musick in so high Estimation, as that, when they would fully Characterise a Learned and Sapient Person, they called him only *ῥητορικὸν*, a Musician: and, if his long Study of Human-
ty

to the Reader.

ty and the Liberrall Sciences had raised Him to Eminency; they onely went two Notes higher, and in the superlative degree styled Him *Μαθηματικος*, as if to be well skilled in the Concordant and Discordant Proportions of Numbers, were the most perfect Diapason of Virtue and Knowledge. Thus much, besides the expresse Records of Plutarch and Diogenes Laertius, may be naturally inferred from hence; that even the best of our Moderne Grammarians, and Philologers derive the word Musick, as also the Muses, from the Greeke Verbe, *μωω*, that signifies to Explore with desire: and this, upon no slender Reason; inso-much as the Key that opens the difficult Locks of all Arts and Sciences, must be an ardent Desire of Disquisition. The same also may bee easily Collected from this Consideration; that to a Complete Musitian
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(please you, to understand Him to be such, as hath not only Nibbled at, but swallowed the whole Theory of Musick; i. e. having profoundly speculated the Pythagorean Scheme of the various Sounds arising from various Hammers, beaten on an Anvill, respective to their different Weights, doth clearly and distinctly understand as well the Arithmetical, as Geometrical Proportions of Consonances, and Dissonances: for, it is not the mere Practical Organist, that can deserve that Noble Attribute) is required a more then superficial insight into all kinds of Humane Learning. For, He must be a Physiologist; that He may demonstrate the Creation, Nature, Proprieties, and Effects of a Natural Sound. A Philologer, to inquire into the first Invention, Institution, and succeeding Propagation of an Artificial Sound, or Musick. An Arithme-

to the Reader.

Arithmetician, to be able to explain the Causes of Motions Harmonical, by Numbers, and declare the Mysteries of the new Algebraical Musick. A Geometrician; to evince, in great variety, the Original of Intervalls Consono-dissonant, by the Geometrical, Algebraical, Mechanical Division of a Monochord. A Poet; to conform his Thoughts, and Words to the Lawes of precise Numbers, and distinguish the Euphonic of Vowells and Syllables. A Mechanique; to know the exquisite Structure or Fabrick of all Musical Instruments, Winde, Stranged, or Tympanous aliàs Pulsatile. A Metallist; to explore the different Contemperations of Barytonous and Oxytonous, or Grave and Acute toned Metals, in order to the Casting of tuneable Bells, for Chimes, &c. An Anatomist; to satisfie concerning the Manner, and Or-

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gans of the Sense of Hearing. A Melothetick; to lay down a demonstrative method for the Composing, or Setting of all Tunes, and Ayres. And, lastly, He must be so far a Magician, as to excite Wonder, with reducing into Practice the Thaumaturgical, or admirable Secrets of Musick: I meane, the Sympathies and Antipathies betwixt Conounds and Dissounds; the Medicomagical Virtues of Harmonious Notes (instanced in the Cure of Sauls Melancholy fits, and of the prodigious Venome of the Tarantula, &c.) the Creation of Echoes, whether Monophone, or Polyphone, i. e. single or Multiplied, together with the Figures of Buildings, and arched Rocks, neer Rivers, Dales, or Woods, requisite to the multiplied Reverberations of Sounds; the Artifice of Otocoustick Tubes, or Auricular Meanders,
for

to the Reader.

for the strengtning, continuation, and remote transvection of weake sounds, and the mitigation of strong; the Model of Autophonous, or speaking Statues; and, finally, the Cryptological Musick, whereby the secret Conceptions of the mind may be, by the Language of inarticulate Sounds, communicated to a Friend, at good distance.

These Considerations præmised; All that can remain to me, as the proper Argument of this Præface, is to advertise you, in a word, (1) That the many and grosse Defects observed in the Latine Impression, especially in the Figures, and Diagramms, wherein the Evidence of each respective Demonstration ought to have consisted; was a principal Occasion to this my English one: which I may justly affirme to be so Accurate, some few Litteral Oversights of the Press only excepted, that the Excellent

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Des-Cartes, had He lived to see it, would have acknowledged the Translator for a greater Friend to his Honour, than that rawe Disciple of his, who having unfaithfully transcribed the Original, and divulged his owne faulty Copy; hath often given occasion not only to the Enemies, but also some of the Defendants of his Masters Learned Industry, to suppose, that in this particular Treatise, He write some things more then Himself clearly understood. And (2) that the Authour of the concise, but weighty ANIMADVERSIONS subsequent, long labouring his Thoughts in the strict Examination of the Apodictical Verity of Des-Cartes, Fundamentals, in this Compendium; most happily lighted on the Discovery of a New Hypothesis, demonstratively sufficient to the full and easie solution of all the Phenomena in Musick:

to the Reader.

a Summary whereof, I doe here, as well to prepare, as endear your Attention, present you.

All Consonances, and other Musical Intervalls doe arise

According to Des-Cartes Principles, from an Arithmetical Division of the Chord, i.e. by Dichotomising the space of an Eighth, &c. as an Eighth from a Bipartition of the whole Line.

According to others, and the most judicious Writers on this Subject (such are Mersennus, Lib. de Instrum. Harmonic. i. propos. 15. & Kircherus, in Artis magn. Consoni & Dissoni Lib. 4.) from the Division of an Eighth Geometrically, i. e. into twelve equal Semitones, by eleven meane Proportionals.

But, according to the New Supposition excogitated by the profound Authour of

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these

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these Animadversions; from the Division of the whole Chord into Extreame and Mean Ration, and of the Mean Ration, according to this Analogie, Viz.

As the Number of Parts in the First Terme,

to the Number of Parts in the Third:

So the Number of Rations between the First and Second,

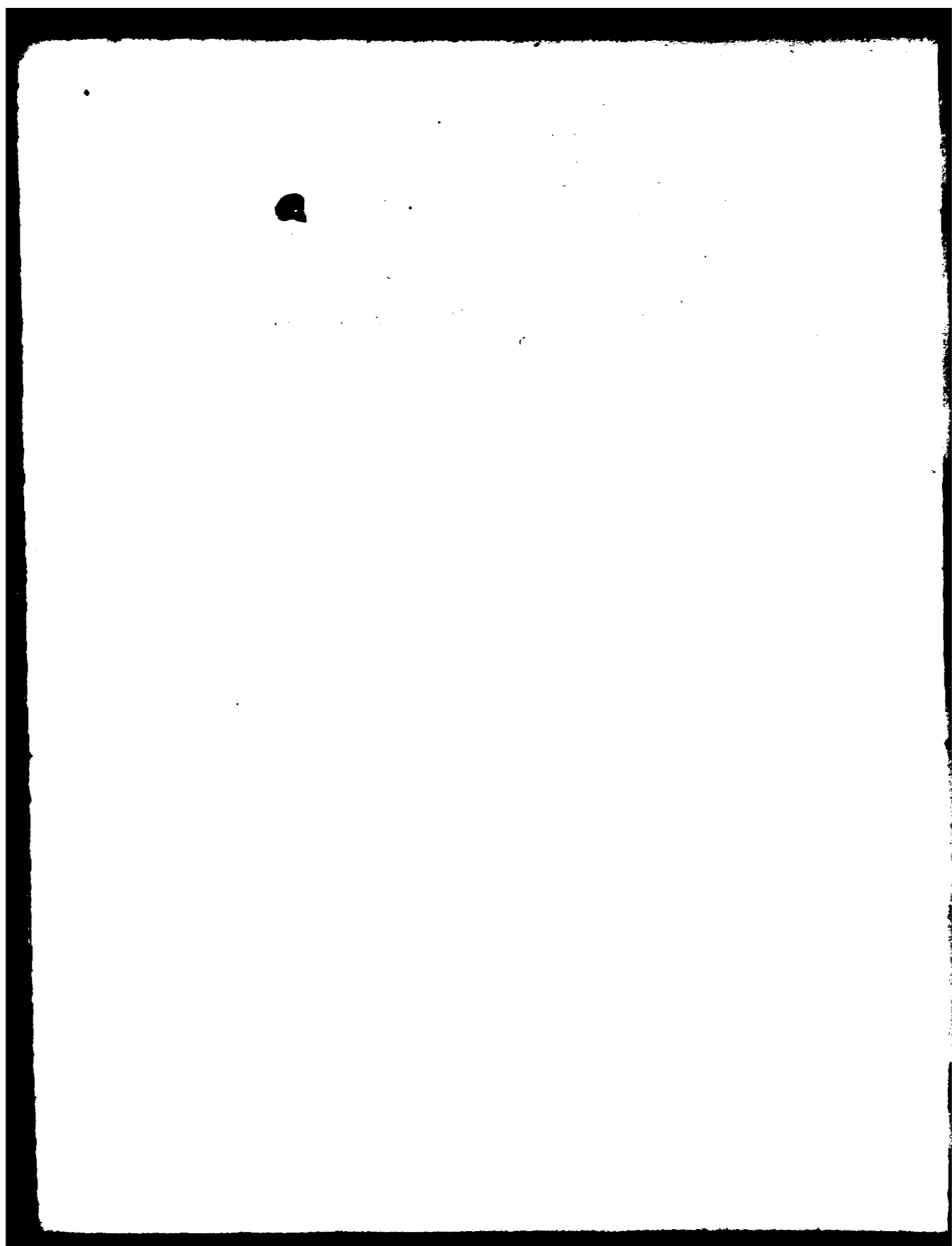
to the Number of Rations between the Second and Third.

Which Novell Invention alone, is more then enough, on the one side, to give the Capable part of Scholers a gratefull Relish of the Inventors extraordinary Abilities in the Noblest Member, or Heart of Learning the Mathematicks: so also, on the other, to promise an advantageous Compensation of so small an expence of Oyle, as is required

to the Reader.

to the comprehensive perusal (not to take notice of the contemptible Price) of these few Sheets. In the Confidence whereof, it is fit I surrender you to the pleasant Lecture and Enjoyment of the Book it self.

A





A Compendium of Musick.

CHAPTER I.

THE *OBJECT* of this Art is a Sound.
 The *END*; to delight, and move various Affections in us. For Songs may be made dolefull and delightfull at once: nor is it strange that two divers effects should result from this one cause, since thus Elegiographers and Tragœdians please their Auditors so much the more, by how much the more griefe they excite in them.

The *MEANS* conducing to this End, or the Affections of a Sound are chiefly two; *viz.* the Differences thereof in the reason of Duration or Time, and in the reason of its intension or modification into Acute or Grave; for concerning the quality of a Sound, from what body and how it may procede more gratefull, is the Argument of Physiologists.

This only thing seems to render the voice of Man the most gratefull of all other sounds; that it holds the greatest conformity to our spirits. Thus also is the voice of a Friend more gratefull then of an Enemy, from a sympathy and dispaty of Affections: by the same reason, perhaps, that it is conceived that a Drum headed with a Sheeps skin yeelds no sound, though stricken,
 A if

if another Drum headed with a Wolfs skin bee beaten upon in the same Room.

C H A P. II.

Præconsiderables.

1. **E** Ach Sense is capable of some Delectation.

2. To this Delectation is required a certain proportion of the object to the sense. Hence comes it, (for instance) that the noise of Thunder, and the report of Guns are not convenient to Musick : because they offend the Ear, as the too great splendor of the Sun doth destroy the sight.

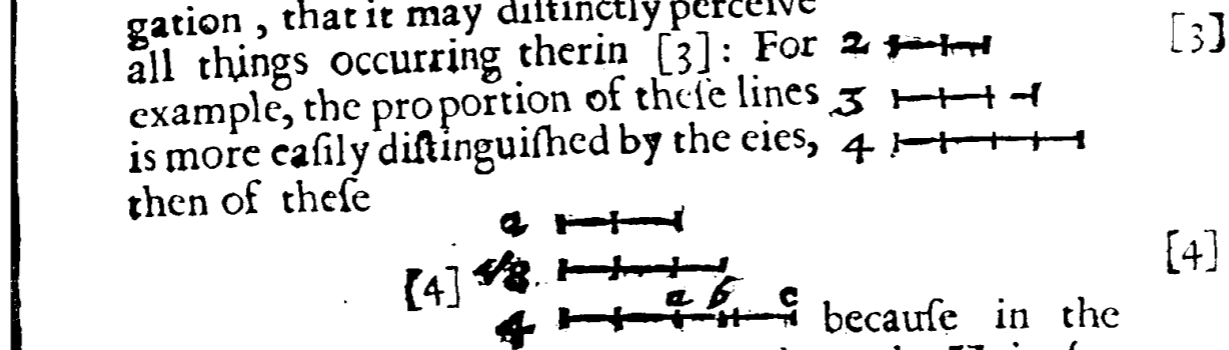
3. The Object must bee such, as that it fall not upon the Sense with too great Difficulty and Confusion. Hence comes it, (for instance) that any Figure exceedingly implicate, though exactly regular, such is the Mother in the Astrolabe, is not so pleasant to the Aspect, as another consisting of lines more equal; such as is in the same Net : the reason wherof is, because the sense doth more fully satisfy it self in the one, then in the other, wherein are many things which it doth not perceive sufficiently distinct.

4. That Object is more easily perceived by the sense, [1] in which is found the least Difference [1] of Parts.

5. The parts of an Object are said to bee lesse different each from other, when they mutually hold the greater proportion [2] each to other.

6. That proportion ought to be *Arithmetical*, not Geometricall. The reason wherof is, because, in that, there

there are not so many things advertible, since the Differences are every where equall: and therefore the sense suffers not so much labour and defatigation, that it may distinctly perceive all things occurring therein [3]: For example, the proportion of these lines is more easily distinguished by the eyes, 4 than of these



because in the first, the sense is required only to advert the Unity for the difference of each line; but in the second, the parts AB, and BC, which are incommensurable. And therefore, I conceive, they can by no means be perfectly perceived by the sense, together and at once, but only in order to a proportion *Arithmetical*; so that it may advert in the part AB two parts, [5] wherof three [6] are existent in BC; wherin it is manifest, that the sense is perpetually deceived.

7. Among Objects of the sense, that is not most gratefull to the Mind, which is most easily perceived by the sense; nor that, on the contrary, which is with the most difficulty apprehended: but that which is perceived not so easily, as that that naturall desire, wherby the senses are carried towards their proper Objects, is not thereby totally fulfilled; nor yet so hardly, as that the sense is thereby tired.

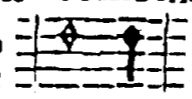
8. Finally, it is to be observed, that *Variety*, is most gratefull in all things. These Propositions conceded, let us consider the first *Affection* of a Sound.

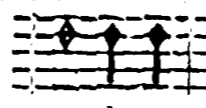
C H A P. III.

Of Number, or Time to be observed in Sounds.

Time, in Sounds, ought to consist of equall Parts; because such are the most easily of all others perceived by the sence, (according to the fourth Praconsiderable:) or of Parts which are in a double or triple proportion, nor is there any further progression allowable; because such are of all others the most easily distinguished by the ear, (according to the fifth and sixth Praconsiderables.) For, if the measures were more unequal, the Hearing could not apprehend their differences without labour and trouble, as experience witnesseth: For, if against one note we should place (for instance) five equall ones; it could not be sung without extream difficulty.

You object, that four Notes may be placed against one, or eight; and therefore a farther progression may be made to these Numbers. We answer, that these Numbers are not the first among themselves, and therefore doe not generate new proportions; but only multiply a double: which is constant from hence, that they cannot be set unlesse combinated, nor can we set such

[7] Notes [7] alone,  where the second is the fourth part of the first:

But thus,  where the last seconds are the half part of the first, and so there is only a double proportion multiplied.

From these two kinds of proportions in Time, there arise

arise two kinds of Measures in Musick: namely by a Division into Three in time, or into Two. But, this Division is noted by a percussion, or stroke, as they call it; which is ordained to assist our Imagination, that so we may the more easily perceive all the members of the Tune, and be delighted with the proportion, which ought to be in them. Now, this proportion is most frequently kept in the members of the Tune, in order to the helping of our Imagination, so that while we yet heare the last of the time, we may remember what was in the first, and what was in the rest of the Tune. Which is effected, if the whole Tune be composed of 8, or 16, or 32, or 64, &c. members: so that all Divisions may proceed from a double proportion. For then, when we have heard the Two first members, we apprehend them as one, while yet wee conjoyne the Third member with the First, so that the proportion becomes triple: afterward, when we have heard the Fourth, we conjoyn it with the Third, and so apprehend it as one and the same. Then we again conjoyn the Two First with the Two Last, and so apprehend those Four together as One. And thus doth our Imagination proceed even to the end: where at length it conceives the whole Tune, as one intire thing composed of many equall members.

Few have understood, how this Measure can be exhibited to the ears without a percussion, or stroke, in Musick, very diminute and of many voyces. This we say is effected only by a certain intension of the Spirit or breath, in *Vocall* Musick; or of the Touch, in *Instrumental*: so as from the beginning of each stroke, the sound is emitted more distinctly. Which all Singers naturally observe, and those who play on Instruments; principally

pally in Tunes, at whose numbers we are wont to dance and leap: for, this Rule is there kept, that we may distinguish every stroke of the Musick, with a single motion of our bodies; to the doing of which we are also naturally impelled by Musick. For certain it is, that a sound doth concusse, or shake all circumjacent bodies, as is exemplified in *Thunder*, and the ringing of *Bells*; the reason whereof is to be referred to the disquisition of *Physiology*. But, insomuch as the *Hoti* is confest by all men, and that the sound is emitted more strongly, and distinctly in the beginning of each Measure, as we have formerly hinted: we may well affirm, that that sound doth more smartly and violently concusse or agitate our Spirits, by which we are excited to motion; as also by consequence, that *Beasts* may dance to number, or keep time with their Feet, if they be taught and accustomed thereto; because to this, nothing more is required, then only a mere naturall *Impetus*, or pleasant violence.

Now, concerning those various Affections, or Passions, which Musick, by its various Measures can excite in us; we say, in the Generall, that a slow measure doth excite in us gentle, and sluggish motions, such as a kind of Languor, Sadnesse, Fear, Pride, and other heavy, and dull Passions: and a more nimble and swift measure doth, proportionately, excite more nimble and sprightly Passions, such as Joy, Anger, Courage, &c. The same may be also sayd of the double kind of percussion, viz. that a *Quadrate*, or such as is perpetually resolved into equals, is slower and duller, then a *Tertiate*, or such as doth consist of Three equal parts. The reason whereof is, because this doth more possesse and imploy the sence, insomuch as therein are more (namely 3) members to
be

be adverted, while in the other are only 2. but a more exact & simple disquisition of this rare secret, doth depend upon the exquisite cognition of the *Motions* of the *Minde*; of which this place is incapable.

However, we shall not omit, that so great is the force of *Time* in Musick, as that it alone can of it selfe adfer a certain *Delectation*; as is experimented in that Military Instrument, the *Drum*, wherein nothing else is required then meerly measure of *Time*; which therefore (I conceive) cannot there be composed of only 2, or 3 Parts, but also of 5, or perhaps 7 others. For since in such an Instrument the sense hath nothing else to take notice of, but bare *Time*: therefore in *Time* may be the greater *Diversity*, that so it may the more exercise and employ the sense.

 C H A P. I V.

Of the Diversity of Sounds, concerning Acute and Grave.

THis may be considered chiefly in three manners, or wayes; either in sounds which are emitted at once and together from divers bodies; or in those which are emitted successively from the same voyce; or lastly, in those which are emitted successively from divers voyces, or sonorous bodies. From the first manner, arise *Consonancies*: from the second, *Degrees*: from the third, *Dissonancies*, which come nearer to *Consonancies*. Where it is manifest that in *Consonancies* the *Diversity* of Sounds ought to be lesse, than in *Degrees*; because that would more tire, and disgust the Hearing
in

in sounds, which are together emitted, then in those that are emitted successively. The same also, in proportion, may be affirmed concerning the Difference of Degrees from such Dissonancies, as are tolerated in relation.

C H A P. V.

Of Consonancies.

First, we are to observe, that an Unison is no Consonance; because therein is no Difference of Sounds, as to Acute and Grave: but that it bears the same relation to Consonances, that Unity doth to Numbers.

Secondly, that of two Terms, required in Consonances, that which is the more Grave, is far the more Potent, and doth in a manner contain the other Term in it selfe: as is manifest in the Nerves of a Lute, of which when any one is percussed, those strings, which are an Eighth, or Fifth more acute [8], tremble and resound of their own accord; but those which are more Grave do not, at least do not appear to the sense so to do; the Reason whereof is thus demonstrated. *One sound bears the same respect to another sound, that one string bears to another string: but in every string that is greater, all the other strings, that are lesse, are comprehended; though every string that is longer, doth not comprehend all the others, that are shorter: and therefore also in every Graver Sound, all others more Acute are comprehended; but not, on the contrary, in every Acuter Sound are the more Grave comprehended: whence it is evident, that the*

the more Acute Terms to be found by the Division of the more Grave. Which Division that it ought to be Arithmetically, *i.e.* into equal parts, is consequent from what was before observed in the sixth Preconsiderable.



Let, therefore, *AB* be the more Grave Term, in which if I would find the Acuter Term of all the first Consonances, I must divide it by the first of all Numbers, *viz.* by 2, as is done in *C*; and then *AC*, *AB*, are distant each from other, the first of all the Consonances, which is called an Eighth and Diapason. Further, would I have other Consonances, which immediately follow the first; I must divide *AB* into three equal parts; and then I shall have not only one Acute Term, but two, *viz.* *AD*, and *AE*, from which there will arise two Consonances of the same kind, *viz.* a Twelfth, and a Fifth. Again, I can subdivide the line *AB* into 4, or 5, or 6 parts, but no further; because such is the imbecillity of the Ears, as that they cannot distinguish, without so much labour as must drown the pleasure, any more Differences of Sounds [9].

[9]

Heer we are required to note, that from the first Division doth arise only one Consonance: from the second, two: from the third, three: as this Table demonstrateth [10].

[10]

B

Fist

First Figure.

 $\frac{1}{2}$ Eighth

$\frac{1}{3}$ Twelfth	$\frac{2}{3}$ Fifth					
$\frac{1}{4}$ Fifteenth	$\frac{3}{4}$ Eighth	$\frac{3}{4}$ Fourth				
$\frac{1}{5}$ Seventeenth Major	$\frac{2}{5}$ Tenth Major	$\frac{3}{5}$ Sixth Major	$\frac{4}{5}$ Tritone			
$\frac{1}{6}$ Nineteenth	$\frac{2}{6}$ Twelfth	$\frac{3}{6}$ Eighth	$\frac{4}{6}$ Fifth	$\frac{5}{6}$ Third Minor		

Here we have not set downe all Consonances that are; in regard, that, to our more facile Invention of the rest, requisite it is that we first treat

CHAP.

C H A P. VI.

Of an Eighth.

THat this is the first of all Consonances, and that which is the most easily perceived by the Hearing after an *Unison*; is manifest from the Premises, and also comprobated by experiment in Pipes: which, when blown with a breath stronger than ordinary, instantly yield a sound more Acute one Eighth. Nor is there any reason, why that sound should immediately arise to an Eighth, rather than to a Fifth, or any other Note; unlesse because an Eighth is the first of all Consonances, and that which is the least different from an Unison. From whence, we conceive, it doth also follow, that no sound can be heard, but it seems in some sort to resound in the ear more Acute an Eighth: and that this is also the cause, why in a Lute to the greater strings, which give Graver sounds, other smaller strings more Acute one Eighth are consociated, which are alwayes percussed at the same instant, and so effect that the Graver sounds are heard more distinctly. Whence it is manifest, that no sound which shall be consonant to one Term of an Eighth, can be dissonant to any other Term of the same Eighth.

A *second* thing to be observed concerning an Eighth, is this; that it is the greatest of all Consonancies, that is, that all other Consonancies are contained therein; or composed [11] thereof, and of others which are contained therein. Which may be demonstrated from hence, that

- [12] all Consonancies consist of equall parts [12]; whence it comes, that if their Terms be more distant each from other than one Eighth, we may, without any further Division of a more Grave Term, adde one Eighth to a more Acute, of which, together with the residue, it will
- [13] appear that that is composed [13]. An Example may be AB , divided into three equall parts, of which AC , AB , are distant by one Twelfth: we say, that Twelfth is composed of an Eighth, and the residue thereof, *viz.*
- [14] a Fifth [14]; for composed it is of AC , AD , which is



- an Eighth; and AD , AB , which is a Fifth: and so it falls out in the rest. Whence it comes, that one Eighth doth not so multiply the numbers of proportion if it compose others, as all others do; and is therefore the only Consonance which is capable of *Gemination*, or *Doubling*. For, if it be *Geminated*, it makes only 4 [15], or 8, if *regeminated*: but if a Fifth be *Geminated*, which is the First after an Eighth, it makes 9 [16]: for from 4, to 6, is a Fifth; in like maner from 6, to 9; which number is far greater then 4, and exceeds the series of the first six Numbers, in which we have [17] formerly included all Consonances [17].

From this it naturally follows; that of all Consonancies, of what kind soever, there are but three Species: one is Simple: another Compound of a Simple and an Eighth: a third composed of a simple and 2. Eighths. Nor can any other Species be added, which is composed of 3 Eighths, and another simple Consonance; because these are the extream limits, nor is there

there any progression beyond three Eighths; since then the numbers of Proportions would be multiplied excessively. From whence is deduced a generall Catalogue of all Consonances whatever, which is here presented in the following Table.

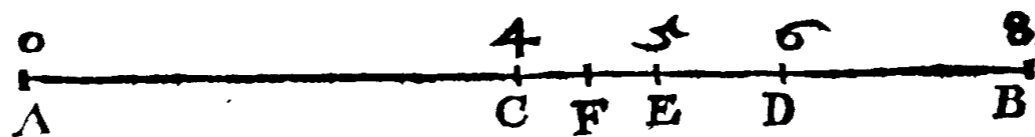
Second Figure.

<i>Eighths</i>	$\frac{1}{2}$	Simple Consonances.	$\frac{1}{4}$	First Compound Consonances.	$\frac{1}{8}$	Second Compound Consonances.
<i>Fifths</i>	$\frac{2}{3}$		$\frac{1}{3}$		$\frac{1}{6}$	
<i>Ditones</i>	$\frac{4}{5}$		$\frac{2}{5}$		$\frac{1}{5}$	
<i>Fourths</i>	$\frac{3}{4}$		$\frac{3}{8}$		$\frac{3}{16}$	
<i>Sixths majors</i>	$\frac{3}{5}$		$\frac{3}{10}$		$\frac{3}{20}$	
<i>Thirds minors</i>	$\frac{5}{6}$		$\frac{5}{12}$		$\frac{5}{24}$	
<i>Sixths minors</i>	$\frac{5}{8}$		$\frac{5}{16}$		$\frac{5}{32}$	

Here have we added the *Sixth Minor*, which we had not observed in the precedent Chapter; in regard it may be educed from what hath been sayd of an Eighth, from which if a Ditone be cut off, the remainder will be a Sixth Minor [18]. But of this more clearly anon.

Wheras we even now affirmed, that all Consonances were comprehended in an Eighth [19]; we are concerned to inquire how that comes to passe, and how they proceed from the Division thereof, that so their nature may be the more plainly and distinctly understood.

First, it is most certain, that that Division of an Eighth, from which all Consonances arise, ought to be Arithmetically, or into equall parts: now what that is, which ought to be divided, is evident in the string AB , which is distant from AC , the part CB ; but the



found AB , differs from the sound AC , an Eighth: therefore will the space of an Eighth be the part CB . That therefore is it, which ought to be divided into two equalls, that the whole Eighth may be divided, which is effected in D [20]. From which Division, that we may understand what Consonance is properly, and *per se* generated; we are to consider that AB , which is the more grave Term, is divided in D , not in order to it self, for then it would have been divided in C , as was done before: nor, as the Case stands now, is an Unison divided,

ded, but an *Octave*, which consists of two Terms, and therefore when the more *Grave* Term is divided, that *Division* is made in order to another more *Acute*. Whence it comes that the *Consonance* properly arising from the *Division*, is between the Terms *AC*, *AD*, which is a *Fifth*; not betwixt *AD*, *AB*, which is a *Fourth*: because the part *DB*, is only the residue, and generates a *Consonance* by accident; from hence, that sound which makes a *Consonance* with one Term of an *Eighth*, ought also to make a *Consonance* with the other.

Again, the space *CB* being divided in *D*, I might by the same reason divide *CD* in *E* [21]; from whence a *Ditone* would be directly generated, and by accident all the other *Consonances*; nor is it requisite that *CE* be further divided; yet if that were done, viz. in *F* [22], then would from thence arise a greater *Tone*, and by accident a lesser *Tone*, and the *Semitones* [23], of which hereafter: for, in a *voice*, they are successively admitted, but not in *Consonances*.

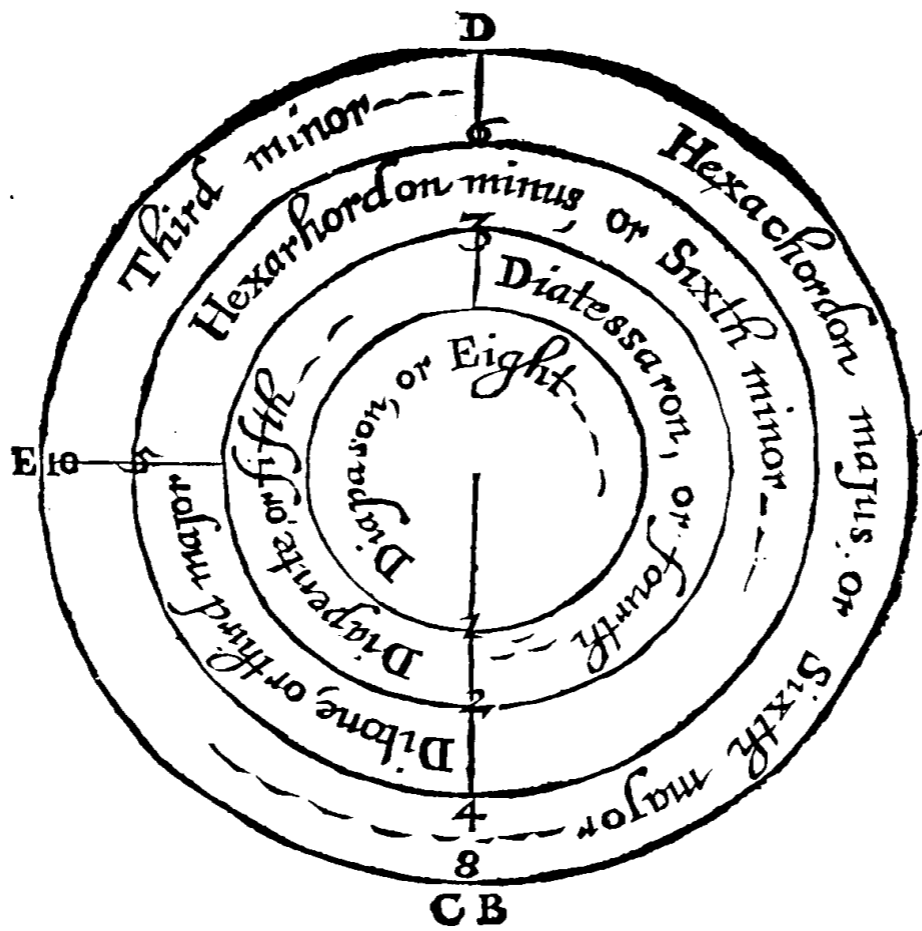
Nor let any think it imaginary, what we say, that only a *Fifth* and a *Ditone* are generated from the *Division* of an *Eighth* properly, and all other *Consonances* by *Accident*; for *Experience* reacheth the same in the strings of a *Lute* or other *Instrument*, whereof if one be *stroke*, the force of that sound will strike all the other strings which shall be more *Acute* in any kind of *Fifth* or *Ditone*: but in the others which are distant a *Fourth*, or other *Consonance*, the same shall not happen. Which force of *Consonances* must undoubtedly arise from hence

hence, either from their Perfection, or Imperfection, in-
somuch as these are first Consonances of themselves, but
all others are only by Accident, because they necessari-
ly flow from others.

But let us enquire, whether that be true, which we
formerly sayd, *viz.* That all Simple Consonances are
comprehended in an Eighth: this we shall easily justi-
fie, if we shall turn CB , the halfe of AB , which con-
tains an Eighth, into a Circle; so that the poynt B may
be joynd to the poynt C . Then let the Circle be divi-
ded in D and E , as it was divided in CB : and the reason
why all the Consonances ought so to be found out, is
because no sound can be consonant to one Term of an
Eighth, but it must also be consonant to the other
Term of the same, as we have already proved. From
whence it comes, that if in the subsequent Figure one
part of the Circle make a Consonance; the residue
must also contain some Consonance.

Third

Third Figure.



From this Figure it is demonstrated how rightly an Eighth is named Diapasson, because it comprehends in it selfe all the intervalls of other Consonances. Here we have exhibited only Simple Consonances; where if we would find out also Compound ones, all we are to do is only to adde, to the intervalls above described, one or two whole Circles; and then it will appear that an

C

Eighth

Eighth doth compose all Consonances.

From what hath preceded, we collect that all Consonances may be referred to Three Kinds; for (1) either they arise from the first Division of an Unison, such are those which are called Eighths, which make the First Genus: or (2) they arise from the Division of an Eighth into two equall parts, such are Fifths and Fourths, which we may therefore call Consonances of the Second Division: or (3) they arise from the Division of a Fifth, which are Consonances of the Third and last kind. We again divide them into such Consonances as arise from those Divisions *per se*; and those which arise *per Accidens*; and that there are only three Consonances *per se* [24], we have formerly sayd, which may be confirmed from the First Figure, in which we extracted the Consonances from the Numbers themselves: For therein we are to take notice, that there are only three sonorous Numbers, 2, 3, and 5 [25], for the number 4, and number 6, are compounded of them, and are therefore sonorous numbers only by Accident, as doth there appear; where, in a right order and a streight line, they do not generate new Consonances, but only such are composed from the former: for example, 4 generates a Fifteenth, and 6 a Nineteenth; but *per Accidens* and in a transvers line, 4 generates a Fourth, and 6 a Third lesser; where we are to observe by the By, that in the Number 4, a Fourth is immediately generated from an Eighth, and is in a manner a certain Monster, or difficient and imperfect Product of an Eighth [26].

CHAP.

CHAPTER VII.

Of a Fifth.

THis, of all Consonances, is the most gratefull, and acceptable to the Ear; and, for that reason, it is the prime and ruling Consonance in all Tunes; as also from it do the *Modes* [27] proceed, as follows from the 7 *Praconsiderable*: for since, as it is manifest from what hath preceded, whether we extract the perfection of Consonances from *Division*, or from *Numbers* [28]; there can properly be found only three Consonances, among which the fifth hath the middle place: this (certainly) is it which resounds in the ears not so sharply as a *Ditone*, nor so languid as a *Diapasson*, but the most pleasant of all others. Further, from the *second Figure* it appears, that there are three kinds of a Fifth [29], where the Twelfth possesses the mean place, which we may therefore affirm to be the most perfect Fifth: from whence it follows, that we might use no other Consonance in Musick, if it were not, as we inferred in the last *Praconsiderable*, that Variety was necessary to *Delectation*.

If it be objected, that, in some cases, an Eighth may be set alone in Musick, without any Variety; as, for Example, when two voyces sing the same Tune, one more acute than the other in an Eighth: but the same doth not evener in a Fifth; and therefore it follows, that an Eighth ought to be accounted the most gratefull of all Consonances, rather than a Fifth.

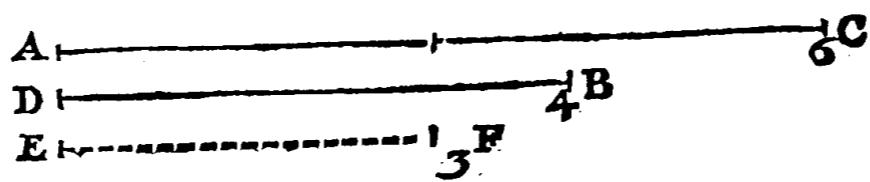
We answer, that, from this Instance, our Assertion is rather confirmed, than infirmed; for the reason, why an Eighth may be so set, is, because it comprehends an Unison in it selfe, and so those two voyces resound in the eare as one; which happens not in a Fifth, whose Terms are more different among themselves, and therefore possesse, and exercise the Hearing more fully; from whence a certain weariness and loathing would arise forthwith, if it were set alone, and without Variety in Tunes. This may be exemplified thus; we should be sooner weary if we were constantly fed with Sugar, and Sweet-meats, than if with bread alone; which every man will allow not, in any proportion, comparable for sweetness and blandishment of the palate, to Sugar.

C H A P. VIII.

Of a Fourth.

THis, of all Consonances, is the most unhappy; nor is it ever used in Tunes, unlesse by Accident, and with the assistance of others: not that it is more imperfect than a Third Minor, or a Sixth, but that it approacheth the nature of a Fifth so neerly, that the grace of this is drowned in the sweetnesse of that. To the understanding of which, we are to note, that a Fifth is never heard in Musick, but that, in some sort, an acuter Fourth is withall advertised; which follows from [30] what we have sayd [30], that in an Unison, there is, in some sort, resounded an acuter Eighth. For Example, let

let AC be in distance from DB of Fifth and the reso-



nance thereof, more Acute by an Eighth, be EF ; and certainly that will be distant from DB , by one Fourth: whence it comes, that it may be called the shadow of a Fifth, which perpetually accompanies it; and thence also it is evident, why a Fourth cannot be set in Tunes, primarily, and *per se*, *i. e.* betwixt a Basse and another part. For when we sayd, that other Consonances were necessary in Musick, only in order to the variation of a Fifth; certainly, it is evident, that a Fourth would be uselesse, in regard it cannot vary a Fifth: which appears from hence; that, if it were set in a more Grave part, it would alway resound more Acute than a Fifth, where the Hearing would soon perceive that it is disturbed from its proper place to an inferiour one, and so a Fourth would be most harsh and unpleasant thereto, as if only the shadow were presented instead of the body, or the Image objected instead of the Thing it selfe.

C H A P. IX.

Of a Ditone, a Third Minor, and Sixths.

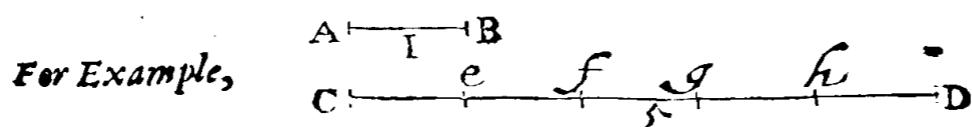
THat a *Ditone* is, by many degrees, more perfect than a *Fourth*, is manifest from the Premises; to which, nevertheless, we shall adde this; that the Perfection of any Consonance is not to be desummed precisely, from the same, while it is Simple; but also from all the Compounds thereof: the reason whereof is, that it can never be heard alone so jejune and empty, but the resonance of this composed is also heard together with it; since that, in an *Unison*, the resonance of a more *Acute Eighth* is contained, we have formerly evicted. Now, that a *Ditone*, so considered, doth consist of lesser Numbers than a *Fourth* [31], and is therefore more perfect than a *Fourth*; is plain from the *Second Figure*: wherein we, therefore, placed a *Ditone* before a *Fourth*, insomuch as we endeavoured, in that *Figure*, to place all Consonances according to the order of Perfection.

But here we are obliged to explain, why the third *Genus* of a *Ditone* is the most perfect, and makes, in the strings of a *Lute*, a Tremulation perceptible even by the sight; rather than the *First*, or *Second Genus*: which we conceive to proceed from hence; that this *Third* doth consist in a *multiplied Proportion*, but the *First* in a *super-particular*, the *Second* in a *multiplied and super-particular*, together [32]. And why, from *multiplied proportion*, the most perfect Consonances do arise; which we therefore placed in the *First* order of the

First

First Figure, we thus demonstrate.

Let the Line *AB* be distant from *CD*, in the Third Genus of a Ditone, howsoever men shall imagine the sound to be perceived by the Hearing; certain it is that it is more easie to distinguish what is the pro-



portion between *AB* and *CD*, than between *CF* and *CD*; because it will first be knowne directly by the application of the sound *AB*, to the parts of the sound *CD*, viz. *Ce, ef, fg, &c.* nor will there be any residue in the end: which falls not alike in the proportion of the sound *Cf*, to *CD*; for if *Cf* be applied to *fh*, there will be the residue *hD*, by the reflection of which we ought to know what is the proportion between *Cf* & *CD*, which is more difficult or tedious. By the same way will it be conceived, if any say that a sound doth strike the ears with many percussions or verberations, and that by so much the more swiftly, by how much the more acute the sound is; for then, that the sound *AB* may arrive at the requisite Uniformity with the sound *CD*, it ought to strike the ears with only five touches or verberations, while *CD* strikes only once: but the sound *Cf* will not so soone returne to an Unifonance, for that cannot be done but after the second stroke of the sound *CD*, as is described in the superiour Demonstration. The same will also be explained, however we conceive the sound to be heard.

A *Third Minor* ariseth from a Ditone, as a Fourth from a Fifth [33], and is therefore more imperfect than

a Fourth, as a Ditone, is than a Fifth. Nor is it therefore to be excluded Musick, since it is not onely not uselesse, but even necessary, in order to the variation of a Fifth. For, since an Eighth is alwayes heard in an Unison, it cannot adfer this variety; nor a Ditone alone, (for there can be no variety unlesse betwixt Two, at least;) therefore is a Third Minor associated thereto, to the end that such Tunes, wherein Ditones are more frequent, may be distinct from such as have a Third Minor very often iterated in them.

[34] A Sixth Major proceeds from a Ditone, and by the same reason participateth the nature thereof, as a Tenth Major, and Seventeenth [34]: to the understanding of which, we are to look back upon the First Figure, where, in the number Foure, are found a Fifteenth, an Eighth, and a Fourth, which is the First Compound Number, and which, by a Binary, (which representeth an Eighth,) is resolved even into an Unity; whence it comes that all Consonances generated from it, are apt and convenient for Composition, among which since a Fourth is found, (which, for that respect, we formerly called a Monster, or defective Eighth;) thence doth it follow, that the same is not unprofitable in composition, where the same reasons do not recur, which hinder it from being set alone; for then is it perfected by the adjunct, and remains no longer subject to a Fifth,

[35] A Sixth Minor proceeds from a Third Minor, in the same manner as a Sixth Major doth from a Ditone [35], and so borrows the nature and affections of a Third Minor: nor is there any reason to countermand it.

Here the Series of Consonances would Exact from us a Discourse concerning their various *Virtues*, as to the excitement

excitement of *Passions*: but a more exact Disquisition of this, may be collected from the Præcedents; and it exceeds the limits of a *Compendium*. For, so various are they, and upon so light circumstances supported; that, a whole Volume would not suffice to perfect their Theory. This, therefore, shall we only say, that the chiefest Variety doth arise from these four last; whereof a Ditone and Sixth Major are more gratefull, more sprightfull, and exhilarating than a Third and Sixth Minor; as hath been observed by *Practical Musicians*, and may be easily deduced from hence, that a Third Minor is generated from a Ditone only by Accident, but a Sixth Major *per se*, because it is no other but a Ditone Compound.

C H A P. X.

Of Degrees, or Tones Musickall.

FOr two causes chiefly are Degrees required in Musick; (1) That by their assistance a Transition may be made from one Consonance to another, which cannot, so conveniently, be effected by Consonances themselves with Variety, the most gratefull thing in Musick: (2) That all that space, which the sound runs over, may be so divided into certain intervals, as that the Tune may alwayes passe through them more commodiously than through Consonances.

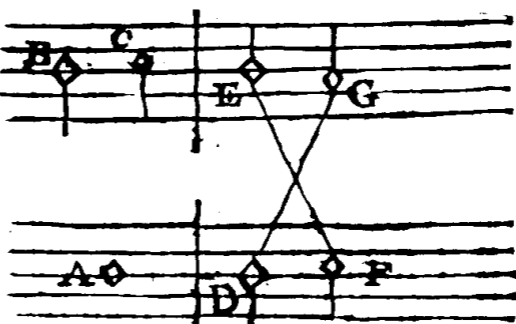
If we consider them in the first capacity; there can be only Four kinds of Degrees, and no more: For then they ought to be desumed from the inequality, found

D

between

[36] between Consonances, and all Consonances are distant each from other $\frac{1}{2}$ part, or $\frac{1}{3}$, or $\frac{1}{4}$, or finally $\frac{1}{12}$; besides the intervals which make other Consonances: therefore all Degrees consist in those numbers, the two first Tones whereof are called Major and Minor, and the two last are called Semitones, Major and Minor. But we are to prove that Degrees, considered in this capacity, are generated from the inequality of Consonances; which is thus done. So often as there is a transition made from one Consonance to another, either one Term is moved single, or both together; and by neither of these two ways can any such transition be made, unlesse by those intervals, which design the inequality betwixt Consonances: Therefore. The first part of the Minor is thus demonstrated.

[37] Let from *A* to *B*, be a Fifth; and from *A* to *C*, be a Sixth Minor; and, of necessity, from *B* to *C* will be that difference, which is betwixt a Fifth and a Sixth Minor, viz. $\frac{1}{12}$ as is evident [38]: but that the



[38] Posterior part of the Minor may be proved, wee are to observe; that wee are not, in sounds, to regard only the proportion while they are emitted together, but also while they are emitted successively, so that, as much as possible, the sound of one Voyce ought to keepe Consonance with the immediately precedent sound of the other voyce; which can never be effected, if the Degrees did not arise from the inequality of Consonances. For Example, let *D E* be a Fifth, and let each Term be moved

moved by contrary motions, so that a Third Minor may be created; if *D F* be an intervall, which doth not arise from the inequality of a Fourth to a Fifth, *F* cannot, by relation, be consonant to *E*; but if yea, then it can: and so likewise in the rest, as may soon be experimented. Here observe, that as concerning that Relation, we sayd it ought to be consonant so much as possible: for alwayes it cannot be, as will appear in the succeeding Discourse.

But if wee consider them in the second Capacity; namely, how these Degrees may, and ought to be ordained in the whole intervall of sounds, that by them one solitary voyce may be immediately elevated, or depressed; then, among the Tones already found out, those Degrees shall only be accounted Legitimate, into which the Consonances are immediately divided. To the manifestation of this, wee are to advert, that every intervall of sounds is divided into Eighths, whereof one can by no means differ from another, and therefore that it is sufficient, if the space of one Eighth be so divided as that all the Degrees may be obtained: as also, that that Eighth is already divided into a Ditone, a Third *minor*, and a Fourth [39], all which evidently follow from what wee have sayd concerning the last Figure of the Superior Tractate. [39]

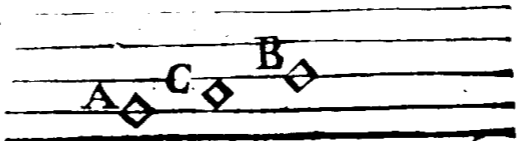
Hence also is it manifest, that Degrees cannot divide a whole Eighth, unless they divide a Ditone, a Third *minor*, and a Fourth; which is thus done. A Ditone is divided into a Tone *major*, and a Tone *minor* [40]; [40] a Third *minor* is divided into a Tone *major*, and a Semitone *major* [41]; [41] a Fourth, into a Third *minor*, and also a Tone *minor* [42], which Third is again divided into a [42] Tone

[43] Tone *major*, and a Semitone *major* [43]; and so the whole Eighth doth consist of three Tones *major*, two Tones *minor*, and two Semitones *majora*; as is manifest to him who seriously and exactly perpend their Scheme. And here we have only three Kinds of Degrees; for a Semitone *minus* is excluded, because it doth not immediately divide Consonances, but only a Tone *minor*. As for Example, if it be sayd that a Ditone doth consist of a Tone *major*, and both Semitones [44] (for both Semitones compose a Tone *minor* [45]): but wherefore, will you say, is not that Degree also admitted, which resulteth from the Division of another, and divides Consonances *onely Mediatly, not immediately*? our Answer is, that the Voyce cannot run through so many various Divisions, and at the same instant be consonant with another different voyce, unlesse with extream Difficulty, as is open to Experiment: besides, a Semitone *minus* would then be joynd to a Tone *major* [46], with which it would create a most unpleasent Dissonance; for consist it would between these numbers 64 and 75 [47], and therefore the voyce could not bee moved through such an intervall. But, in order to the clearer solution of this Objection, we are to note;

That to the Creation of an Acute sound, is required a more forcible emission of the breath, or spirit in v-call Musick; or a stronger percussion of the strings in instrumentall; than is required to the Creation of a Grave: which is experimented in the strings of a Lute, which yield a sound by so much the more Acute, by how much the more they are distended; as also from hence, that by a greater force, the Aer is divided into lesser parts, from which the more Acute sound must of necessity

necessity be generated: and from hence it is a direct
 Consequence, that by how much the more Acute a
 sound is, by so much the more strongly doth it strike
 the eares. From this animadversion, I conceive, a true
 and chiefe reason may be rendred, wherefore *Degrees*
were invented, viz. least, if the voyce should run through
 the Terms of Consonances alone, there would bee a-
 mong them too great a disproportion in the reason of
 intension, which would inevitably tire both the Audi-
 tors and Singers. For Ex-

ample, would I ascend
 from *A* to *B*, because the
 sound *B* will strike the ears



far stronger, than the sound *A*, lest that Disproportion
 should be incommodious, the Term *C* is set in the middle,
 by which we may, as by a Degree, more easily, and with-
 out that inequall contention of the breath, ascend to *B*.
 From which it is manifest, that Degrees are nothing els
 but a certaine *medium*, interposed betweene the Terms of
 Consonances, for the moderation of their inequality; and
 that of themselves they have not sweetnesse enough to
 satisfie the eares, but are only considerable and usefull in
 order to Consonances; so that while the Voyce runs
 through one Degree, it leaves the Hearing unsatisfied,
 untill it shall have arrived at a Second; which, for that
 respect, ought, together with the former Degree, to con-
 stitute a Consonance: and this is sufficient to solve the
 praecedent Objection. Moreover, this also is the reason,
 why, in a Voyce, successively Degrees are admitted, ra-
 ther than Ninths or Sevenths, (which arise from De-
 grees,) or others which do consist of lesse Numbers than
 Degrees; namely, because intervals of this sort do not

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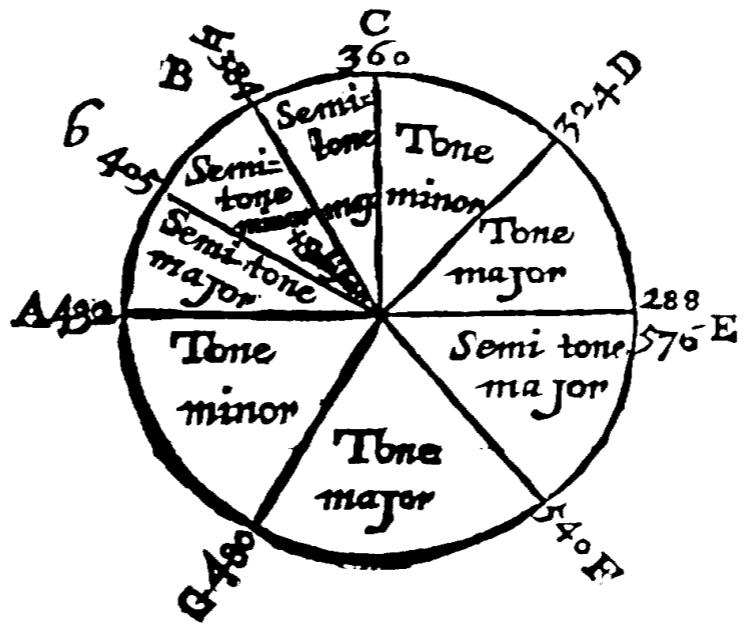
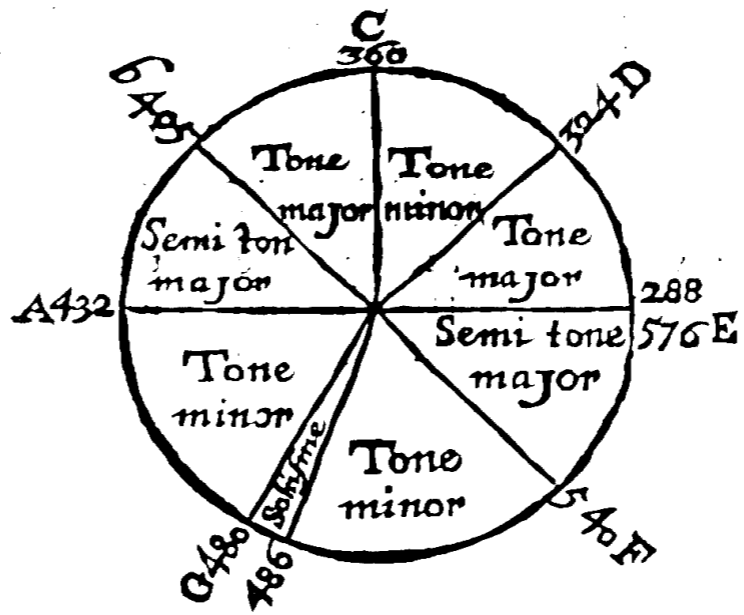
divide

divide the least Consonances, nor can they therefore moderate that inequality, which is betwixt their Terms. More, concerning the invention of Degrees, (which arise from the Division of a Ditone into two parts, as a Ditone doth from the Division of a Fifth,) might be super-added; and many things from thence be deduced, which concern their sundry *Perfections*: But it would require more room than a *Compendium* can afford, and a good Understanding may infer as much, from what hath preceded concerning *Consonances*.

More requisite it is, that, in the present, we speak of the Method or Order, in which those Degrees are to be constituted in the whole space of an Eighth; now this Order ought to be such, as that a Semitone *major*, may have on each side next to it a Tone *major* [48]; as also a Tone *minor* [49], with which this doth compose a Ditone; and the Semitone a Third *minor*, according to what we have just now observed [50]: but since an Eighth containeth Two Semitones, and as many Tones *minor*; that this may be obtained without Fraction, it ought also to containe Four Tones *major* [51]: Now because it containes only three, therefore is it necessary, that, in some place, wee use a certaine Fraction, which may be the difference betwixt a Tone *major* and a Tone *minor*, which we nominate a *Schism* [52]; or also between a Tone *major* and a Semitone *major*, which contains a Semitone *minus* with a *Schism* [53]: to the end, that by the helpe of these Fractions the same Tone *major* may, after a sort, bee made moveable, and so perform the office of two Tones; which is easily preceptible
in

in the Figures here delineated, where we have turned the whole space of an Eighth into a Circle, after the same manner, as in the end of the Sixth Chapter.

And truly in either of these Figures, every intervall designeth one Degree, except Two: viz. a Schism in the First, and a *Semitone minus* with a Schism in the Second: which Two are in some sort moveable, so that they may bee referred successively to both Degrees immediately annexed unto it.



Now,

Now manifest it is from these Figures (1) That, in the First Figure, there can be no addition by Degrees from 288 [324] to 405, unless wee chuse the middle Term, in respect of the middle Term, for that in it respect 288, it may seeme to be 480, but if it respect 405, then it may seeme to be 486, viz. that with both it make a Third *minor*, and the difference is so small betwixt 480 and 486, that the mobility of that Terme, which is continued from both, shall not strike the Hearing with a Dissonance perceptible.

[54]

(2) In the Second Figure, after the same reason, we cannot ascend from the Terme 480 to 324 by Degrees, unless wee use the middle Terme, as that, if it respect 480, it may seeme 324, if it respect 324, it may be 405, that is, which both may make a Ditone. But because betwixt 324 and 405, the difference is so great, that no voyce can be so tempered as that if it hold a Consonance with one of the extremes, but it will appeare exceedingly Dissonant from the other: therefore is another way to be sought, by which (the most of all others) this so great an incommodity may be, if not totally removed, yet at least greatly diminished. Now this can be no other way, but what is found and described in the Superior Figure, viz. by the use of a Schism: by this means, if wee would goe through the Terme 405. Wee will remove the Terme G, by one Schism, that it may be 486, no more 480: and if wee would goe through 384, we will change the Terme D, and 320 shall be in the place of 324, and so shall be distant, by a Third *minor*, from 384.

E

From

From these considerations it is evident, that all the spaces, through which one voyce solitary may be moved, are contained in the First Figure: for, when the incommodity of the Second Figure is corrected, then
 [55] doth it not differ from the First [55]; as is easily comprehended.

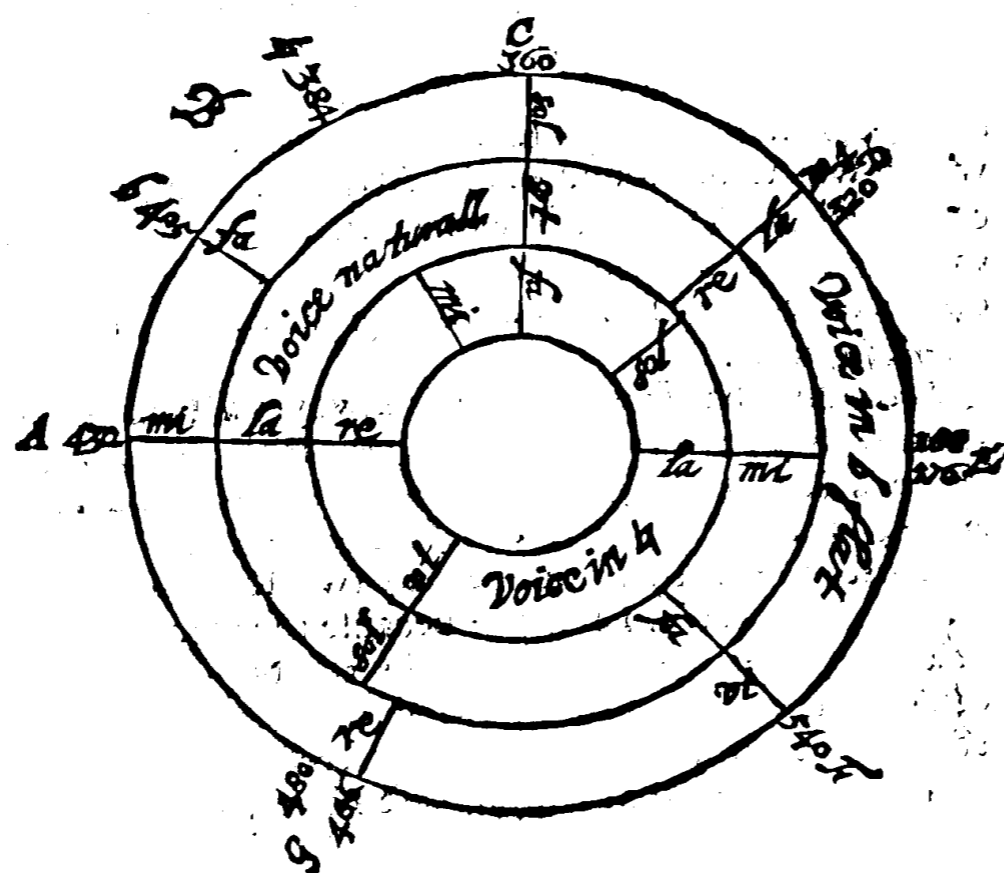
Evident it is also, that that Order of Tones, which practical Musicians call the *Hand*, doth contain all the Modes, by which Degrees may be obtained; for, that they are comprehended in the two precedent Figures, is formerly proved: and that *Hand* of Practical Musicians doth contain all the Termes of each Precedent Figure, as is easily discerned in the following Figure, in which we have turned that *Hand*, into a Circle, that so it might the better be referred to the Superiour Figures. Yet, to the understanding of this Figure, we are to signifie, that it begins from the Term *F*, where, for that cause, we have applyed the greatest number, that thence it might be collected that that Term is of all the
 [56] most *GRAVE* [56].

Figure

of MUSIC.

35

Figure the Sixth.



That it ought to be so, is inferred from hence ; that we can begin Divisions from onely two places of the whole Eighth : so that therein eisher two Tones may be set in the first place , and, after one Semitone, three Tones consequent in the last place ; or, on the contrary, three Tones in the first place, and only two in the last. And the Term *F* representeth both those two places together

A COMPLETION

gether. For, if from thence we go by *b*, only two Tones, are in the first place, but if by *a*, there will be three: Therefore,

First, then it is manifest from this Figure, & the second precedent, that only five Spaces are contained in a whole Eighth, by which the voyce can naturally proceed, *i. e.* without any Fraction, or moveable Terme, which was to be found but by Art, that it might proceed further. Whence it came, that those five inter-vals should be attributed to a Naturall Voyce, and six only Voyces were found out to expresse them; *viz. ut, re, mi, fa, sol, la.*

Secondly, that from *ut* to *re*, is alwayes a Tone minor; from *re* to *mi*, alwayes a Tone major; from *mi* to *fa*, alwayes a Semitone major; from *fa* to *sol*, alwayes a Tone major; and lastly from *sol* to *la*, a Tone minor.

Thirdly, that there can be only two Kinds of an Artificiall Voyce, *viz. a and n*: because the space betwixt *A* and *a*, which is not divided in the Naturall voyce, can only be divided by two Modes; so as that a Semitone be set in the first place, or the second.

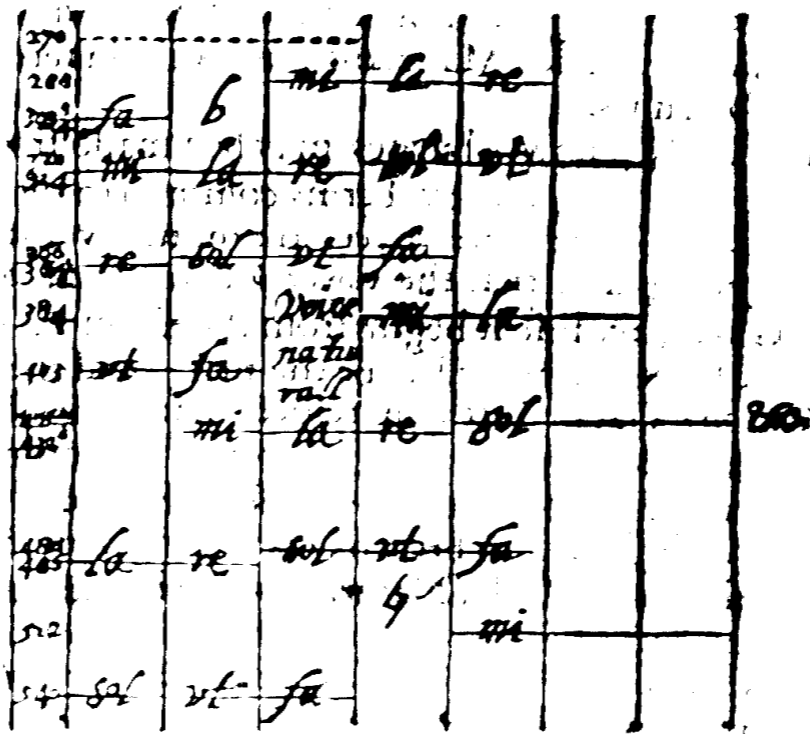
Fourthly, for what reason these Notes, *ut, re, mi, fa, sol, la*, are againe repeated in those Artificiall Voyces: for Example, for, when wee ascend from *A* to *a*, inso-much as there are not other Notes, but *mi* and *fa*, to signifie a Semitone minor, it thence follows, that in *A*, *mi* is to be set, and in *a*, *fa*, and so in other places in order. Nor can you say, it had been more convenient to have invented other Notes; for they would have been superfluous, since they must have designed the same intervals, which are designed by those Notes in a Naturall voyce; besides they would have been inconfund-ous,

ous, because so great a multitude of Notes must have exceedingly troubled Musicians; as well in seeing, as singing of Tunes.

And lastly, how changes may be made from one voyce to another: viz. by 1. an interval common to two voyces: as also that these voyces are mutually distant by a Fifth [57]; and that the voyce *b* Flat is all the most Grave, because it begins from the Termination, which we have formerly proved to be the *b* Flat, and therefore it is called *b* Flat or Soft, in respect that by how much any Tone is the more Grave, by so much is it the more soft and remisse. For to the emission thereof is required the lesse spirit, or breath, as we have more then once intimated. And a Naturall voyce is and ought to be a mean, nor could it rightly be called *Naturalis*, if the voyce were to be elevated, or depressed beyond Mediocrity, in the expression thereof. Finally, the voyce *d*, is called a Quadrate, or Sharp, because it is the most A-
[58] *phoides* in Eighth into a Tritone and a Fifth take [58], and is therefore lesse sweet than *b* Soft.

Some perhaps will object, that this *Hand* is not sufficient to comprehend all the Changes of *Diaptes*; for, as in it is shewn, how freely we may depart from a Naturall voyce, either to *b* Soft, or to *d*; so also ought other collateral Orders to be designed therein, such as are seen in the Section *Pignit*; that it might have been free for *b* also to be taken from *b* Soft, as the Naturall voyce, or to the other part, and so from *d*; which is confirmed from hence, that Musicians in Practice frequently use such intervals, which they explicate either by *Diaptes*, or by *b* Soft; which the other (b) are separate from its proper Seat.

A COMPRENDIUM



To this we return that by this means might be made a progresse, *usq; ad infinitum* : but, in that *Hand*, ought to be expressed the Changes of only one Tune ; and that those are contained within three Orders, is demonstrated from hence, that in every Order only six Terms are contained, of which two are changed, when a change is made to the following Order, and so there remain therein only Four Termes of those, which were in the former ; but if a Transition bee againe made to a Third Order, then will two Degrees of the four precedent ones bee changed, and so there will remain onely two of those which were in the former Order, which would lastly be taken away in the fourth Order, if the progresse should be continued unto it, as is visible in the Figure:

Figure, whence it is most evident, that the Tune would not be the same it was in the beginning, if from thence it would remaine in the same Term unchanged. And what is added concerning the use of Diesis; I say, that they doe not constitute whole Orders, as *b* Soft, or *p*, but consist only in one Terme, which they elevate (as I conceive) by one Semitone *mi*, all the other Terms of the Tune remaining unchanged; now the manner how, and the reason why this is done, I doe not at present so well remember, as to be able sufficiently to explain; nor why, when only one Note is elevated above *la*, a *b* Soft is usually affixed unto it: which I think may easily be deduced from Practice, if the Numbers of those Degrees, in which they are used, and of voyces, which with them make Consonances, bee subducted; and the matter I judge well worthy a serious Meditation.

Finally, here it may be objected, that six voyces, *ut*, *re*, *mi*, *fa*, *sol*, *la*, are superfluous, and only Four may suffice; since there are only three divers intervals: by which way that any Musickall Tune can be sung, I deny not. But because there is great difference betwixt the Terms Grave and Acute; and a Grave Terme, as is formerly noted, is much the chiefest: therefore is it better and more commodious to use divers Notes, than the same towards an Acute part, and towards a Grave part.

This place requires us to explain the *Practica* of these Degrees, how Musickall parts are constituted of them, and by what reason ordinary Musick composed by practick hands may be accommodated to what of the Theory hath been premised; that so all Consonances and other its intervals may bee exactly calculated. In
order

16

COMPEAD 14

and so we know, that
 the distance between any two
 chords added, is the tone of the
 distance between them; and that these tones are distant
 each from other, two Degrees; and therefore that be-
 twixt any two chords, one other is always to be under-
 stood, which is musical for us, and constant in us. As
 again, since all the lines are equally distant each from
 other, but signify unequal spaces: therefore are Two
 Marks invented, b and β , one whereof is set in the
 chord, which represents the Term B (as β in the
 because one Tune doth frequently consist of many parts,
 which parts are separately described; as is not yet
 known, from these marks, b and β , which of these man-
 ny parts is superior, and which inferior; and therefore
 are there three other Marks found out. γ , δ , ϵ the or-
 der whereof we have formerly observed [59]. Now, that
 all these things may be the more manifest, we have
 here placed this following Figure, in which we have
 expressed all the Chords, and removed them each from
 other more or less, according to the greater or lesser
 spaces which they denote [60]; that so the proportion
 of Consonances might be presented together to the eye.
 Besides, we have made this Figure double, that the
 Difference between b and β , might be visible; nor can
 those Tunes, which are to be sung by one, be described
 by the other, unless all the Tunes of the b be removed
 by a Fourth or Fifth, from their proper Seat, so that
 where stands the Term F or γ , there is to be set G or
 δ .

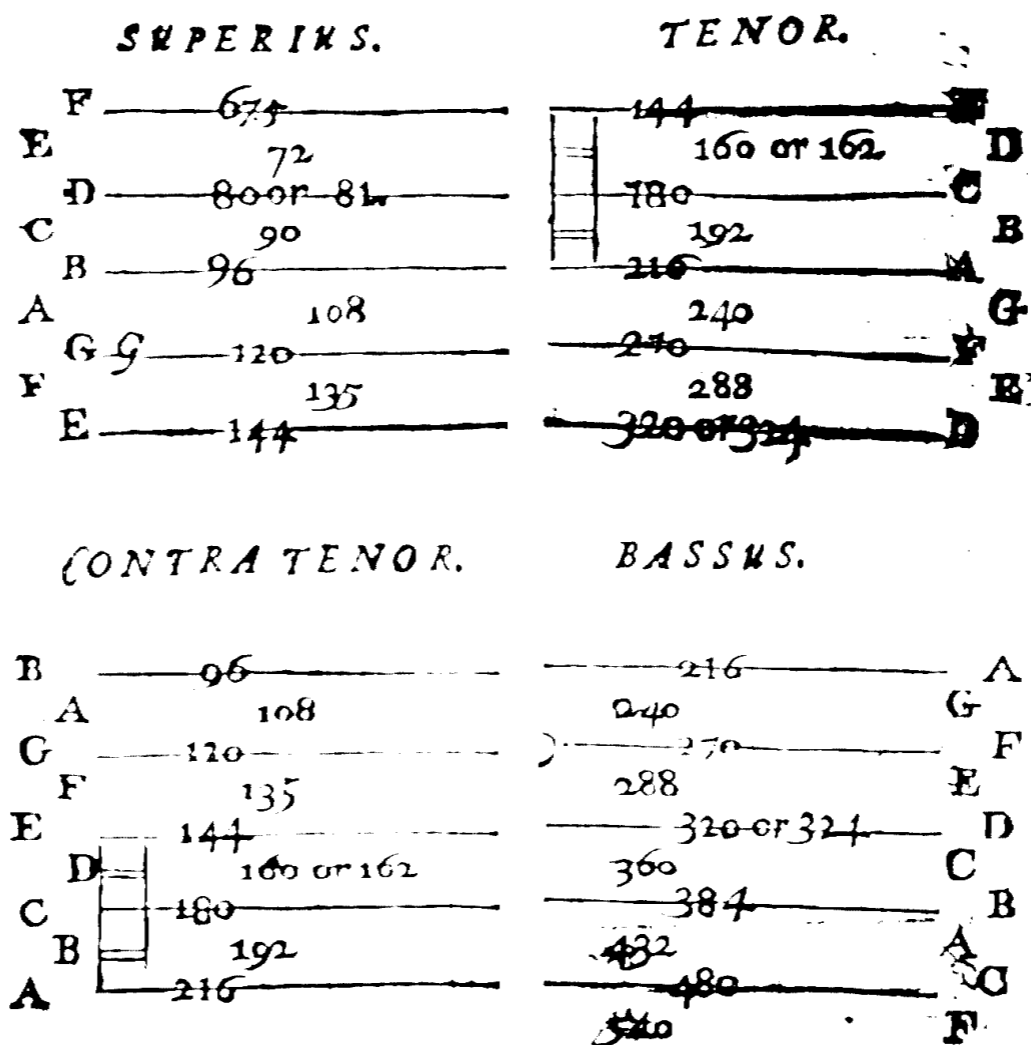
Further

6 flat		4 sharpe	
B		fa	72
B		sol	80 or 81
C		fa	90
B	b	ma	96
A		re	108
G	g	sol	120
F		fa	135
E		ma	144
D		fa	160 or 162
C	#	sol	180
B	b	fa	192
A		ma	216
G		re	240
F	f	re	270
E		re	288
D			320 or 324
C			360
B	f	86c	384
A		405	432
G		432	480
F		480 or 486	480
E		540	540

Further than this we are not to goe, for these ought to be the Terms, since they divide three Eights, within which all Consonances are included, to which the Practice of Musicians doth accord, for they hardly ever exceed this space.

F

Superius.



Now the use of these Numbers is, to teach what proportion all the Notes hold among themselves, such as are contained in all the parts of one Tube: for the sounds of these Notes hold the same proportion one to another, as the numbers appoyed on the same Chords. So as if the string be divided into 540 equal parts, and the sound thereof represent the most Grave Term F:

48 parts of the same string will yield the sound of the Term G; and so consequently.

And here we have ordered 4 degrees of Parts, that it might appear, how much they ought to be distant each from other; not that the Cliffs), Ξ , and ζ are not often set in other places, which is done according to the variety of Degrees, which are run over from each part: but because this Mode seems to be the most Naturall, and is the most frequent.

Again, here have we set Numbers only in the Naturall Chords, and so long as they are not removed from their proper seat; but if Dieses be found in some notes, or *b*, or \flat , which may remove them from their proper seats: then are those to be explicated by other Numbers, whose quantity is to be deduced from other Notes of other Parts, with which these kinds of Dieses make a Consonance.

C H A P. XI.

Of Dissonances.

AL L other Intervalls, except those of which we have now spoken, are called Dissonances; but we will treat of those only, which are necessarily found in the newly explicated order of Tones, so as they cannot but be made use of and applyed.

Of these there are three kinds [61]: (1) Some are generated from Degrees only, and an Eighth: (2) Others from the difference which is betwixt a Tone *major* and *minor*, which we have denominatèd a Schism: and

[62] (3) others from the Difference, which is between a Tone major, and a Semitone *majus* [62].

In the *First Genus*, are contained *Sevenths* and *Ninths*, or *Sixteenths*, which are only *Ninths* compounded, as *Ninths* are nothing else but *Degrees* compounded of an *Eighth*, and *Sevenths* nothing but the residue of an *Eighth*, from which one *Degree* is detracted; whence it is manifest, that there are three divers *Ninths*, and three *Sevenths*, because there are three kinds of *Degrees*; and all these consist betwixt these Numbers [63]:

A	}	<i>Ninth maxim</i> ; <i>Ninth major</i> ; <i>Ninth minor</i> ;	}	<i>Seventh major</i> ; <i>Seventh minor</i> ; <i>Seventh minim</i> ;
---	---	--	---	--

Among *Ninths*, two are *majors*, which arise from two *Tones*, the First from a *major*, the Second from a *minor*, for the distinction of which we have noted one *Ninth maxim*: on the contrary there are two *Sevenths minors*, for the same reason, and therefore we have called one *Seventh minim*.

Now, that these *Dissonances* cannot be avoyded in sounds successively emitted, among divers parts is most clear: yet haply any one may enquire, why they ought not to be admitted in a voyce successive of the same part equally with *Degrees*, since it is evident that some of them are explicated in lesser Numbers than the *Degrees* themselves, and therefore may seem to be more gratefull to the Hearing than *Degrees* [64]. The solution of which Doubt doth depend on this, which we have before observed, that a voyce [65] doth require so much the

the more intension of the spirit or breath, by how much the more Acute it is, and therefore Degrees were invented, that they might be *Means*; betwixt the Termes of Consonances, and that by them wee might the more easily ascend from the Grave Terme of any Consonance to the Acute of the same, or *vice versa*, descend from the Acute to the Grave Terme which cannot be performed by Sevenths or Ninths; as is evident from hence, that the Termes of these are more distant each from other, than the Termes of Consonances are, and therefore they would be emitted with a greater inequality of Contention.

In the *Second Genus* of Dissonances do consist a Third *minor*, and a Fifth Deficient by one Schisme; as also a Fourth, and a Sixth *major* increased by one Schisme. For since (necessarily) there is one moveable Terme by the intervall of a Schisme, in the whole Series of Degrees; it cannot be avoyded, but that, from thence, such Dissonances in relation, *i.e. in voce successive emissa a diversis vocibus*, will be generated: And that more then these now named cannot arise from thence, may be proved by induction [66]. These consist in these Numbers [67]:

{	<i>Third minor defective</i>	—————	27	
			32	
	<i>Fifth defective by one Schism</i>	—————	27	[66]
			40	[67]
A <	<i>Fourth increased by one Schism</i>	—————	20	
			27	
	<i>Sixth major increased by a Schism</i>	—————	4816	
			8127	
			F 3	Or

[68]

Or thus [68]:

Third interval of a <i>Schisma</i>	C ad D. 480, 405.
by a <i>Schisma</i>	D ad E. 384, 324.
Fifth interval of a <i>Schisma</i>	G ad D. 480, 324.
Fourth interval of a <i>Schisma</i>	D ad G. 324, 240.
Sixth interval of a <i>Schisma</i>	b ad G. 405, 240.
by a <i>Schisma</i>	D ad b. 324, 192.

But so great are these Numbers, that such intervals cannot be collected of themselves; but, as we have formerly noted, because the interval of a *Schisma* is so small, as it can hardly be discerned by the ears, therefore do they borrow sweetness of those Consonances, to which they are nearest. Nor do the Terms of Consonances so consist in *indivisibili*, as that if one of them be a little changed, all the sweetness of the Consonance must instantly be lost: and this can only be the reason, why *Dissonances* of this *second genus* may be, in a voice successive of the same part, admitted in place of Consonances, from which they are divided.

In the *Third Genus* are contained, a Tritone, and a Fifth false; for in this, a *Semitone major* is accounted for a *Tone major*; but in a Tritone, the Contrary: and they are explicated by these numbers [69]:

[69]

Tritone $\frac{32}{45}$ Fifth false $\frac{45}{64}$

Or

Or thus [70]:

[71]

Tritone { F ad. pl. 340, 384. }
 { b ad E. 405, 288. }

Fifth false { d ad F. 384, 270. }
 { e ad b. 288, 202; vol 576, 495. }

Which Numbers are also too great to explicate any intervall which may not be ingrate to the ears; nor have they any Consonances very near, from which they may borrow sweetnesse; as the Precedent ones have. Hence comes it, that these last Dissonances ought to be avoided in relation; at least, when slow and soft Musick is made, and not diminute; for in very diminute Musick and such as is sung swiftly, the hearing is too much employed to take notice of the defects of such Dissonances: which defect is much more evident, from hence, that they are near to a Fifth, with which the hearing therefore compares them, and, from the preceptious sweetnesse of this, doth the more clearly discern the imperfection of those.

Here we shall end our explication of all the Affections of a Sound; having first only taken notice, in order to the probation of what we formerly said, that all the Variety of sounds, as to Grave and Acute, doth arise in Musick onely from these Numbers 2, 3, and 5. We say that all numbers, by which as well Degrees as Dissonances are explicated, are composed of those three, and by them, division being made, may at length be resolved even to an unity.

CHAP.

C H A P. XII.

Of the reason of composing.

From the Premises it followes, that we may, without any great error or solcecism, compose Musick, if we observe these 3 axioms.

1. That all sounds which are emitted together, may be distant each from other, in any Consonance, except a Fourth, which lowest ought not to be heard, *i.e.* against a Basse.
2. That the same voice be moved successively, only by Degrees, or Consonances.
3. Lastly, That we admit not a Tritone, or Fifth false, no not so much as in relation.

But, for the greater Elegancy and Concinnity, we are to note these following Rules.

1. That wee begin from some one of the most perfect Consonances; for, so is raised a greater attention, than if some jejune and frigid Consonance led up the Van: or else, most gratefully, from a pause or silence of one voyce; for when, immediately upon the silence of one voyce, which began the Tune, another unexpected one First invades the ears, the novelty thereof doth by a kind of potent charm, conjure us to attention. Now, concerning a Pause we have been hitherto silent, because of it self a Pause is nothing, but onely induceth a certain novelty and variety, while the voyce, which was silent, doth againe begin to sing.
2. That two Eights, or two Fifths never immediately

ately succeed each other. The reason why that is prohibited more expressly in these Consonances than in others, is because these are the most perfect, and therefore when one of them is heard, then is the Hearing therewith fully satisfied, and unless the attention be presently removed from that to another Consonance, it is wholly occupied by the pleasantness thereof, so that it can little regard the variety, and the (in some sort) frigid Symphony of the Tune; which happens not in Thirds and other Consonances, no though they be reiterated, for in all others the attention is still kept up, and a desire encreased of expecting a more perfect Consonance.

3. That so much as possible, the parts goe on in contrary motions, in order to the greater variety: for then both the motion of every voice is distinguished from the adverse voice, and Consonances are distinguished from other Consonances near them. Also that all the voyces be moved oftner by Degrees, than by leaps.

4. That, when we would advance from any lesse perfect to a more perfect Consonance, wee alwayes defect to one that is near, rather than to one that is remote; for example, from a Sixth *major* to an Eighth, from a Sixth *minor* to a Fifth, &c. understanding the same also of an Unison and the most perfect Consonances. Now, the reason why this method is to be observed in progression from imperfect to perfect Consonances, rather than *e contra*, from perfect to imperfect; is, because, when we heare an imperfect Consonance, the eares are induced to expect a more perfect one, wherein they may receive more satisfaction, and to this expectation are they carried by a certain naturall violence: and there-

fore ought a more vicine, than a remote Consonance rather to be set, that being what the Hearing desires. But, on the contrary, when a perfect Consonance is heard, we expect no imperfect one. Yet this Rule is subject to frequent variation, nor can we now call to mind, from what to what Consonances in particular, and by what motions we ought to pervene: all these depend on experience, and the practice of Musicians; which being known, we conceive it no difficulty to deduce the reasons and proportions of all from this our Theory of Musick: and I have formerly deduced many of them, but my peregrinations have worn them out of both my Papers and Memory.

5. That, in the end or close of each Tune, the eares be so fully satisfied, as they expect no more, but perceive the Tune to be perfect: which is most conveniently effected by some Orders of Tones alwayes ending in a most perfect Consonance, which Orders Musicians call Cadences, all the Species of which Cadences have been copiously enumerated by *Zarlino*. Who hath Generall Tables or Schems also, wherein are described what Consonances in particular ought to succeed each other through a whole Tune; of all which hee hath given some reasons, but we believe that more and more plausible ones, may be deduced from our Fundaments.

6. And lastly, that the whole Tune together, and every voyce seperately be included within certain limits, which are called Modes, of which anon.

All these Rules are to be exactly observed in the Counter-poynt of only two, or more voices; but not in a Diminute, nor any way varied: for in Tunes very Diminute, and (as they call them) Figurate, many of them

them are remitted. Which that we briefly explicate, wee are concerned first to treat of the foure Parts, or Voices used in Tunes; for though in some are found more, in some fewer Symphonies: yet that seems to bee the most perfect and most usuall Symphony, which is composed of four Voices.

The First and most Grave of all these Voices, is that which Musicians call *Bassm.* This is the chiefe, and ought principally to fill the ears, because all other Voices carry the chiefe respect to the *Basse*, the reason whereof we have formerly declared. Now, this Voice is wont to move on not onely by Degrees, but also *per Saltum*; the reason is, because they were invented to ease that trouble, which would arise from the inequality of the Terms of one Consonance, if one should immediately bee expressed upon the neck of another; since the more Acute doth strike the eare much more forcibly than the Grave. For this trouble is lesse in a *Basse*, than in other parts; in respect that it is the most Grave, and therefore requires lesse strength of the spirit or breath to its effusion, than any other. Besides, since all other Voices hold a respect to the *Basse*, as the principall; it ought to strike the ears more sensibly, that it may bee heard more distinctly: which is effected, when it moves on *per Saltum*, i. e. by the Terms of lesser Consonances immediately, rather than when it moves on by Degrees.

The Second, being the next to the *Basse*, they call *Tenor*; this being also, in its kind, the chiefe, because it contains the Subject of the whole Modulation, and is comparatively the Nerve, which extended through the body of the Tune, doth sustain and conjoyn all the rest of its Members. And therefore it is wont, so much as possible,

possible, to move on by Degrees; that so its parts may be the more united, and the Notes of it may be the more easily distinguished from the Notes of other Voices.

To the *Tenor* is opposed the *Contra-tenor*; nor is it used in Musick for any other reason but because, by progressing to contrary motions it may occasion Variety, and so Delight. It is wont, as the *Basse*, to move on by leaps; but not for the same reasons: for this is done only for convenience and variety; for it consists betwene two voices, which move on by Degrees. Practisers so compose their Tunes sometimes, that they descend below a Tenor; but this is of small moment, nor doth it seem at any time to adfer any novelty, unlesse in imitation, consequence, and the like artificiall counter-poynts.

Superius is the most Acute voice, and is opposed to *Bassus*, so that by contrary motions they frequently occur each to other. This voice ought chiefly to incede by Degrees; because, since it is most Acute, the difference of Terms in this would cause greater trouble and difficulty, if those Terms, which it would successively emit, were at too great distance each from other. And it is wont to be moved the swiftest of all others in Diminute Musick: as the *Counter-Basse* most slowly: the reasons whereof are deduceable from our precedent discourse; for a more remisse sound strikes the Ears more slowly, and therefore the Hearing cannot endure so swift a mutation therein, in respect it would not have leasure to hear all the single Tones distinctly.

These things thus explained, we are not to omit, that in these Tunes Dissonances are frequently used instead of Consonances; which is effected two wayes, viz. by
Diminution

Diminution, or Syncope.

1. *Diminution* is when against one Note of one part, are set 2. or 4. or more in another; in which this order ought to be kept, that the First make a Consonance with a Note of another part, but the Second, if it be only one Degree distant from the former, may make a Dissonance; and also be, by a Tritone, or Fifth fals, distant from another part, because then it seems there set only by accident: and as a way, by which wee may come from a First Note to a Third, with which that First Note ought to make a Consonance, as also doth the Note of the opposite part. But, if that Second Note incede *per Saltus*, i. e. be distant by the intervall of one Consonance from the First; then ought it to make a Consonance also with the opposite part: for the former reason ceaseth. But then a Third Note may make a Dissonance if it be moved by Degrees; of which let this be an Example.

The musical notation consists of two staves. The top staff is labeled 'Superius.' and the bottom staff is labeled 'Bassus'. Both staves show a sequence of notes with a triplet of three notes. The Superius part has a triplet of three notes, and the Bassus part has a triplet of three notes. The example shows how the second note of the triplet in the Superius part is a tritone from the first note of the triplet in the Bassus part, creating a dissonance. The notes are labeled with letters: B, D, F in the Superius part and G, A, E in the Bassus part. The triplet is marked with a '3' and 'etc.' below it. The example is labeled 'Exemplum.' and 'Syncope.p.'.

A *Syncopa* is, when the end of one Note in one voice is heard at the same time with the beginning of one other Note of an advers part; as may bee seene in the Example set, where the last time of the Note *B*, is dissonant with the beginning of the Note *C*, which is therefore brought in, because there is yet remaining in the eares the recordation of the Note *A*, with which it made a Consonance; and so *B* bears it selfe to *C*, only as a Relative voyce, in which the Dissonances are carryed through: yea, the Variety of these doth cause, that the Consonances, among which they are set, are heard more distinctly, and also excite the more constant attention. For, when the Dissonance *B C* is heard, the expectation of the eare is encreased, and the judgement of the sweetnesse of the Symphony somewhat suspended, untill the Tune shall arrive at the Note *D*, in which it more satisfies the Hearing; and yet more perfectly in the Note *E*, with which, after the end of the Note *D*, hath kept up the attention, the Note *E*, instantly supervenient doth make an exquisite Consonance, for it is an Eighth [71]. And, indeed, therefore are these Consonances used in Cadences; because what hath been the longer expected, doth the more please when it comes: and therefore the sound, after a Dissonance heard, doth better acquiesce in a most perfect Consonance, or Unison. But heere Degrees are to be set betwixt Dissonances: for whatever is not a Consonance, ought to be accounted a Dissonance.

Moreover, wee are to observe, that the Hearing is more satisfied in the end by a Eighth, than by a Fifth, and best of all by an Unison; not because a Fifth is not gratefull to the eare, as to the reason of Consonance:
but

but because in the end we are to regard Quiet, which is found greater in those sounds, betwixt which is lesse difference, or none at all, as in a Unison. Now this Quiet, or Cadence is delectable not only in the end: but also in the middle the avoidance of this Cadence introduceth no small delight; namely, when one part seems willing to quiesce, and another proceeds on. And this is a kinde of Figure in Musick, such as are Rhetoricall Figures in Oration, of which sort are *Consequence, Imitation, &c.* which are effected, when either two parts successively, *i. e.* at divers times, sing wholly the same, or a quite Contrary, which at last they are wont to doe. And truly this, in certain parts of a Tune, doth sometimes much advantage Musick; but as for those artificiall *Counter-points*, as they call them; in such Compositions where that Artifice is observed perpetually from the beginning to the end: we conceive, they may belong not more to Musick, than *Acrosticks*, or retrograde Verses to Poesie, which was invented to charm the mind into respective passions, as well as Musick.

C H A P. XIII.

Of Modes.

Frequent it is among Practitioners to treat of these Modes, and what they are, all well know; therefore would it be superfluous here to insist thereon: we shall observe only, that they have their originall from hence, that an Eighth is not divided into equall Degrees, for one while a Tone, another while a Semi-tone

tone is found therein : and besides , from a Fifth, because that of all others is most acceptable to the eare, and every Tune seemes to bee composed for the sake of this alone : for an Eighth can be divided into Degrees, onely seven different wayes [72], every one of which [73] may bee againe divided by a Fifth two wayes [73], except Two [74] ; in one of which is found a Fifth false in place of a Fifth [75], whence there ariseth onely twelve Modes, of which foure are lesse elegant, for this [76] cause, that a Tritone is found in their Fifths [76], so as they cannot, from a Fifth principall, and for whose sake the whole Tune seemes composed, ascend or descend by Degrees, but of necessity there must occur a false Relation of a Tritone, or a Fifth false.

In every Mode, are three principall Termes, from which all Tunes ought to bee begun, and most chiefly [77] concluded [77], as all Musicians know : and they are called Modes as well from hence, that they restrain the Tune, least the parts of it ramble beyond mediocrity to excess; as from hence chiefly, because they are apt to containe various Tunes, which may diversly affect the minde according to the variety of Modes ; of which many things have been sayd by Practisers, taught onely by experience, the reasons of all which may be deduced from our precedent discourse : for, certaine it is, that in some many Ditones, or Thirds *minors*, and in places more or lesse principall, are found, from which almost all the variety of Musick doth arise, as hath beene formerly proved. Again, as much may be sayd of Degrees themselves ; for a Tone *major* is the First, and comes nearest to Consonances, and is *per se* generated from the [78] Division of a Ditone ; but all others *per Accidens* [78],
from

from which and the like, many things concerning the nature of Moods might be deduced, if a *Compendium* would permit. And here it should follow, that we should discourse of all the motions of the mind, which may be excited by Musick, and in a singular Treatise shew, by what Degrees, Consounds, Times, &c. those motions ought to be excited: but I should be constant to my purpose of writing an Epitome.

I now discover Land, hasten a shoare, and omit many things for brevity, many by oblivion, but more by ignorance. However, I suffer this issue of my braine, so inform, and lately brought forth rude as a Bears Cub, to venture abroad into your presence: that it may remain as a Monument of our Familiarity, and a most certain memoriall of my love of you: yet, if you please, upon this condition, that, being confined to the secreete of your Closet, it be not exposed to the Judicature of others, who may not (as I trust you will) avert their benevolous eyes from the maimed, and defective parts of this Exercise, upon those others, in which I deny not but I have expressed some Lineaments of my Ingénit to the life: nor would they know that this *Compendium* was composed for your sake alone, by one who could not obtain Privacy in an Army, nor leisure in a Throng of other Cares and Affairs.



CONTENTS.

C H A P.

- I. **I**ntroduction.
- II. **P**reconsiderables.
- III. **O**f the Number, or Time to be observed in Musickall sounds.
- IV. **O**f the Diversity of Sounds; concerning an Acute and Grave.
- V. **O**f Consonances.
- VI. **O**f an Eighth.
- VII. **O**f a Fifth.
- VIII. **O**f a Fourth.
- IX. **O**f a Ditone, a Third minor, and a Sixth major, and minor.
- X. **O**f Degrees, or Tones Musickall.
- XI. **O**f Dissonances.
- XII. **O**f the Reason of Composing.
- XIII. **O**f Modes, alias Moods.

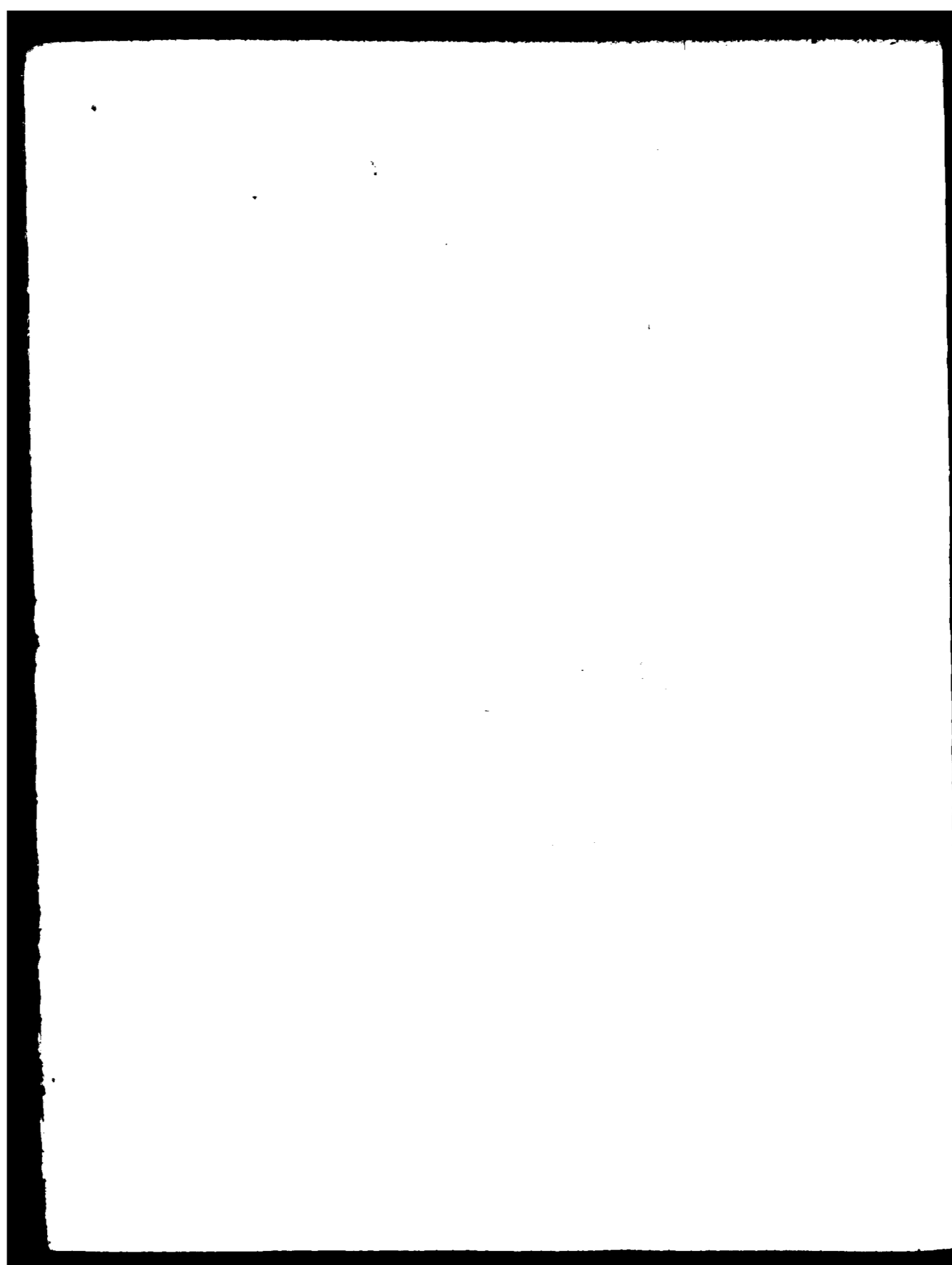
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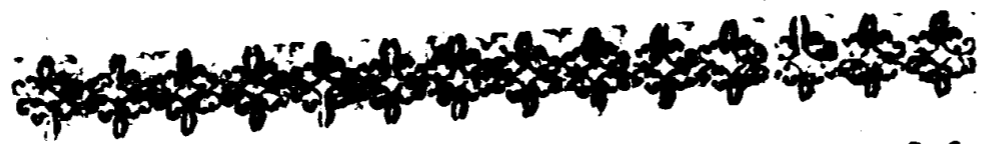
ANIMADVERSIONS
UPON THE
Musick-Compendium
OF
RENAT. DES-CARTES.



L O N D O N,

Printed by *Thomas Harper*, for *Humphrey Moseley*, and
are to be sold at his Shop at the Sign of the *Prin-*
ces Armes in *S. Pauls Church-Yard*. 1653.





Animadversions upon the Musick-Compendium of R. Des-Cartes.

In these Subsequent Animadversions, brevitatis gratia,

Characterize	Roote, or Side	√
	Addition, or more	+
	Subduction, or less	-
	Equality	=
	Aggregate, or Sum	Σ
	Excess, or Difference	X
	Lower, or Greater	∇
	Lower, or Greater Term	∇
	Higher, or Acuter	Δ
	Higher, or Acuter Term	Δ
	Ration	R
	A quality of Ration, or proportionall	::
	Continued Proportion	∴
	Multiplyer, or multiplyed by	m
	Divisor, or divided by	n
Product	∩	
Quotient	∪	
Paraph	∩	
Logarithms	∩	

thus:

And, *distinctionis causa*, I denominate the first Note or Term of any Consonance, or other Musically Intervall, an *Unison*; and the other, according to its difference, in sound, from the former.

[1] Audible Differences are as visible Ratios: For Sounds cannot be distinguished, or their Differences known otherwise than by their mutuall habitude. understand me as thus: The *sounds of strings* are according to their *Ratios*, not visible *Differences*: for Example, as these three Chords have $a \text{---} 12 \text{---} \text{Unison}$.
 an equality of Ratios: (for $b \text{---} 12 \text{---} \text{Eighth R.}$
 $a. b. :: b. c.$) so their Sounds $c \text{---} 4 \text{---} \text{Fifteenth R.}$
 (an *Unison*, *Eighth*, and
Fifteenth) have an equality of Differences. (For $1+7 = 8$,
 and $8+7 = 15$.) And as these $d \text{---} 12 \text{---} \text{Unison}$
 three Chords have an inequality $e \text{---} 13 \text{---} \text{Fifth}$.
 of Ratios: (though an equality $f \text{---} 8 \text{---} \text{Eighth R.}$
 of Differences visible; for
 $d+g = e$, and $e+g = f$.) so their Sounds (an *Unison*,
Fifth, and *Eighth*) have an inequality of Differences *audible*. For as the Ratio of d to e , is $2:3$ (and $2:3$ is a *Fifth*,
 by Fig. first, p. 10.) so the difference of an *Unison* and a
Fifth is a *Fifth*. ($1+4 = 5$.) and as R. of e to f is $4:5$: (and
 $4:5$ is a *Fourth* by Fig. first, p. 10.) so the difference of a
Fifth and an *Eighth* is a *Fourth*. ($5+3 = 8$.) And (there-
 fore) Sounds, thus numbred, are as it were imperfect
 (because not equally distant) audible Indices,
 or Logarithms of their Chords. Here the Reader may
 observe that for the Difference of an *Eighth*, I have ad-
 ded

ded only seven; of a Fifth, four; and of a Fourth, three: and the reason is, because the exclusive account is alwayes one lesse than the inclusive, as is made visible *Animad. 8.*

[2] *Viz. Arithmetical.* Whereof on strings are two sorts; one *audible*, the other *visible*; but, as to their measure, the *Last* only is properly called *Arithmetical*; the first *Rationall*, or *Geometrical*.

[3] Note there are in *Sounds* two *Proportions*, and *Progressions*, as well as in *Lines* and *Numbers*; *viz.* the *Arithmetical*, as *Second*, *Third*, and *Fourth*: for $2 - 1 = 3 - 2 = 1$; and the *Geometrical*, as *Second*, *Third*, and *Fifth*: for $1. 2 :: 2. 4$. And note also, as was sayd before *Animad. First*: That when *Strings* are *audibly* in an *Arithmetical* proportion, or progression, they then are *visibly* in a *Geometrical*; whence I infer that *Chords*, as to *Sounds*, ought to be *Geometrically* divided, not *Arithmetically*; because, so divided, the sense of hearing has not so much to advertise; the *audible Differences* being alwayes equal, &c. whereof more, after *Anim. 78, P. 1.*

$$[4] \sqrt{8} = 2.828+, \text{ therefore is } \begin{cases} a b = 0.828+ \\ b c = 1.172- \end{cases}$$

[5] *Viz.* 0.8.

[6] *Viz.* 1.2.

[7] The *Notes*, or *Markes of Time*, in *Musick* are thus Named,

Named,	Large	—	Fourd,	Valued.
	Long	—		
	Briefe	—		
	Semibriefe	—		
	Minim	—		
	Crotchet	—		
	Quaver	—		
	Semiquaver	—		

But note these Markes are found otherwise valued sometimes; as when a Large doth comprehend three Longs, a Long three Briefes, &c. according to their severall Moods; or Moods, Times, and Prolations: For satisfaction wherein, as in all things else practical in Musick, not necessary to be known, as to the understanding of this Compendium, the Reader is referred to *Harmonicon Mersenni*, *Musurgia Kercheri*, *Morley's Introduction*, &c.

[8] That is, is Four or Seven Notes higher: For the Fifth is the Fourth from the First, and the Eight is the Seventh, &c. The knowledge of which Notes, together with all other Consonances, and Muscull Intervalls (some few excepted, not now in use,) may bee, without difficulty, obtained by inspection on the first Figure following.



Whitcomb

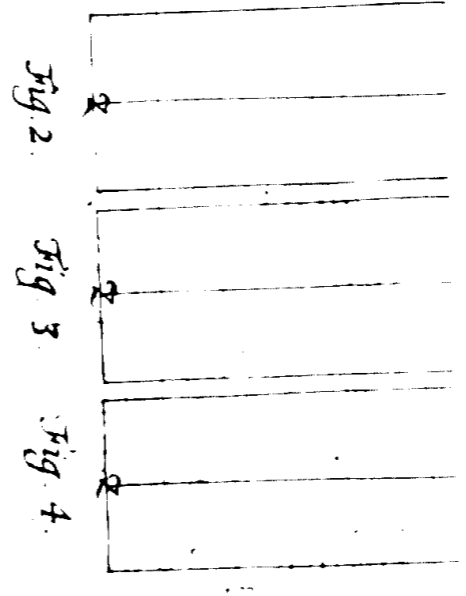
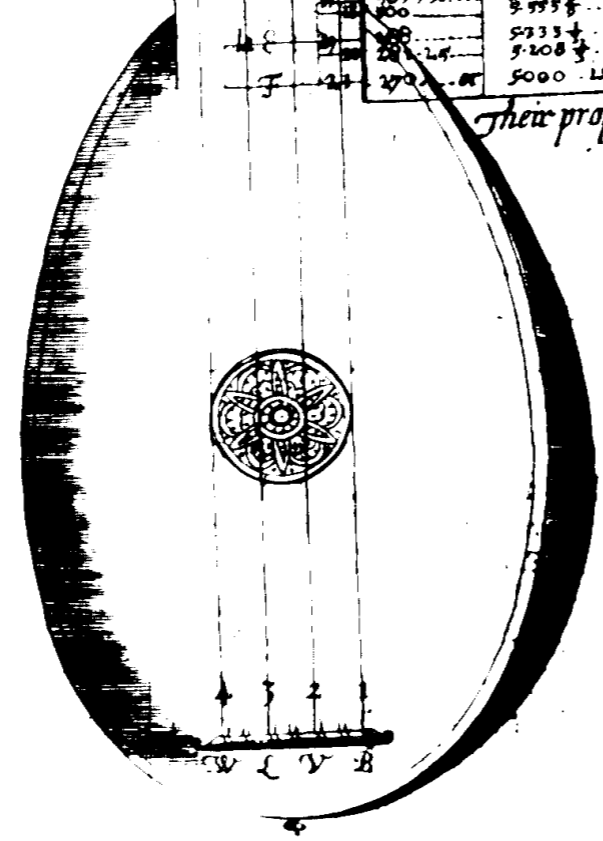
Whereof the *Space* from the *Bridge* to the *Nut*, is understood to be divided into 540, or 10'000 equall parts: the Number of which parts (accounting from the *Bridge*) to each actuall division of the foure Chords, or *Strings*, numbred at the *Bridge* 1, 2, 3, 4; is to be found on the *Right hand*. The first (B 0) presents you all the *Intervalls* under an *Eighth*; and their proportions, names, and differences by parallell entrance thence towards the *Right hand*. and is thus to be read: viz. B 0 [540, or 10'000], is to B 1 [518'4, or 9'600], as 25, to 24: as an *Unison*, to its *Acuter Semitone minus*: B 0 [540, or 10'000]. B 2 [506'25, or 9'375] :: 16.15 :: *Unison*. Δ *Sem. major*: B 21 [270, or 5'000]. B 20 [281'25, or 5'208 $\frac{1}{2}$] :: 24.25 :: *Unison*. ∇ *Sem. minor*: B 21 [270, or 5'000]. B 19 [288, or 5'333 $\frac{1}{3}$] :: 15.16 :: *Unison*. ∇ *Semt. major*: The *Habitude*, or Proportion of B 1, to B 2; or of B 2, to B 1: or the difference of a *Semitone minor*, and *major*; or of a *Seventh major*, and *Semi-Eighth*; is a *Diesis minor*, &c. Hence it appeareth that B 0, if struck, when stop'd at 1, doth sound a *Semitone minor* more acute, than it doth, if struck, when unstop'd or open: and that a *Semitone minor* (as 01) is equall to $\frac{1}{25}$ of the ∇ , and is subtracted from it; and $\frac{1}{16}$ of the Δ , and is added to it. And the like (*mutatis mutandis*) in all the Rest.

The *Second Chora* (VF) is divided according to b flat: the *Third* (LF) according to \sharp shape: both, from F to F, as in the *Scale*, P. 41. And the *Fourth* (WA,) as these, and the like *Instruments*, are usually fretted.

Thus having all the *Intervalls* under an *Eighth*, those above are easily known: for they are all compounded either of one, or more *Eighths* only; as the *Fifteenth*, *Two & twentieth*, *Nine and twentieth*, &c. or else of one, or more *Eighths*, and some one of these. And (therefore) as B 0 was divided, to make the first seven Notes after, or above the *Unison*, so is B 21 understood be divided, to make the seven next after, or above the *Diapason*, &c. ad infinitum.

Animadversions upon the
Their proportions, Denominations,

	1000	10000	12	15	20	as an Interval, to its acuter
B	1000	9600	27	24	24	Semitone major; or Diatic major
B	1000	9375	16	15	15	Semitone major; or Diatic minor
C	1000	8000	12	9	8	Tone or second major; or Diatic major Tone or second major; or Diatic minor
D	1000	6250	8	6	5	Third minor; or Schisma Third minor; or Semiditone
E	1000	5000	5	4	4	Third major; or Ditone
F	1000	4000	3	2	2	Fourth, or Tetrachord Fourth + Schisma
G	1000	3000	2	1	1	Fifth Semitone
A	1000	2000	1	1	1	Sixth - Schisma Sixth; or Diapente
B	1000	1500	2	1	1	Sixth minor; or Diapente + Semit. major Sixth major; or Diapente - Tone minor Diapente + Tone major
C	1000	1000	1	1	1	Seventh minor; or Diapason - Tone major Seventh minor; or Diapason - Tone minor
D	1000	750	1	1	1	Seventh major; or Diapason - Semitone major Semi. eighth
E	1000	500	1	1	1	Eight; or Diapason



Their propor.

Musick-Compendium of R. des-Cartes

Differences.

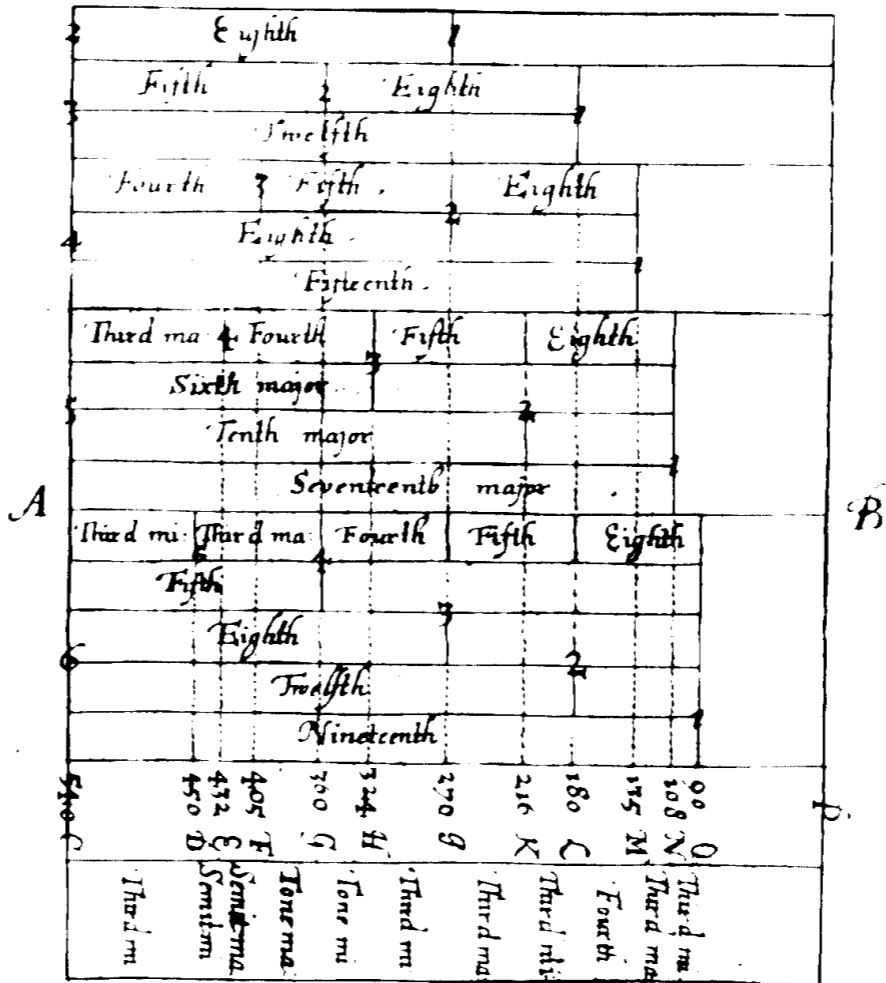
1	2	Eight, or Diapason	
26	46	Semi-Discrete	Semitone minor, or Chromatica
8	19	Seventh major	Semitone major, or Chroatica
5	26	Seventh minor	Semitone minor
9	16	Seventh mixture	Semitone major, or Chromatica
16	27	Eighth + Second major	Semitone major, or Chromatica
3	9	Sixth major	Semitone major, or Chromatica
5	8	Sixth minor	Semitone minor
27	37	Fifth - Schisma	Semitone major
64	69	Fourth - Schisma	Semitone minor
32	43	Fourth	Semitone major
20	27	Third + Schisma	Semitone major
4	9	Third major	Semitone major
5	6	Third minor	Semitone minor
26	32	Third minor - Schisma	Semitone major
8	9	Second major	Semitone major
9	10	Second minor	Semitone minor
15	16	First major	Semitone major
16	17	First minor	Semitone minor
25	26	Unison to its grave	Semitone major

tions, Denominations, Differences.

410210000	410210000	410210000
910389450	909789439	909289429
482288920	481188909	480188898
455788458	454188409	452788358
430687974	428687977	426987905
405987479	404187462	402987454
384987120	381887071	379687029
365586728	360486674	357986628
348586298	340286300	337586250
333985823	321185946	318285895
321685308	303185622	300185557
311584869	286185297	282985244
303684417	270184900	266884941
297883962		251884559
294083504		237884195
291383044		223783822

Animadversions upon the

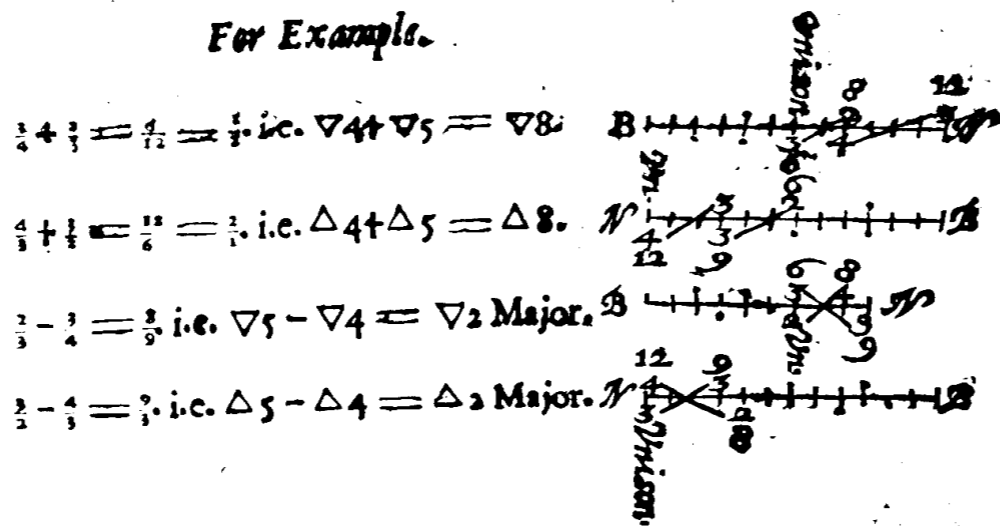
- [9] Yett, in his Second figure p. 13, y^e Author set's downe some Consonances with greater Differences; and page. 14. he dichotomiseth A B in to eight parts for the Consonances, as into 16 for both Tones.
- [10] But more clearly this fig: followiug, where the Space. A B is actually and distinctly divided into 2, 3, 4, 5, & 6, equall parts.



[11]. All Harmonicall Compositions are performed by Addition of their

their *Ratios*, and Divisions by Subduction: *viz.*
 Addition, by a Multiplication of the *like* Terms, or
 Collaterally thus =:
 Subtraction by a Multiplication of the *unlike* Terms,
 or obliquely thus X:

For Example.



as is visible from the divisions on the *seare* Chordes ad-
 joyning.

[12.] As may be seen in Fig. An. 10.

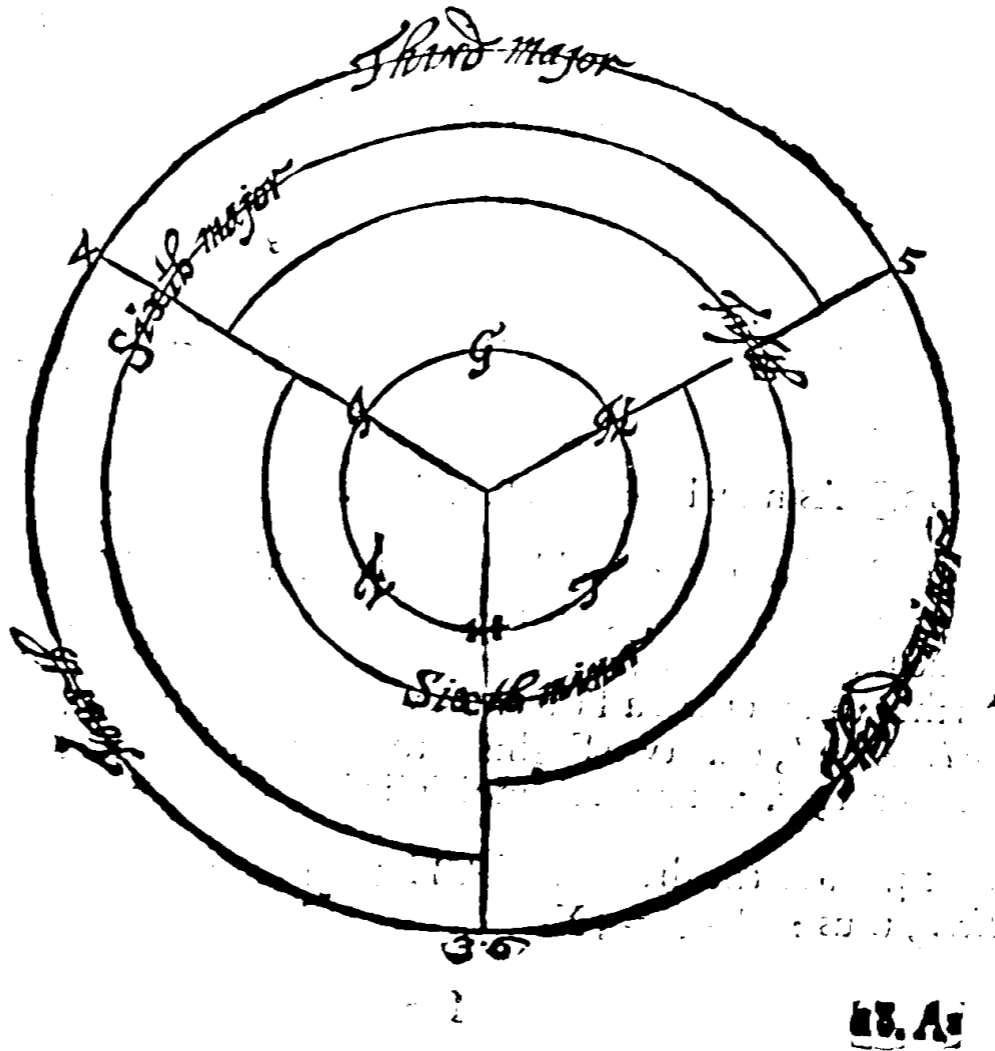
[13.] That is, the double of the lesser Term, with the
 greater, giveth the excess thereof above an *Eighth*, *viz.*
 if the Intervall exceedeth not a *Fifteenth*: but if they be
 further distant than a *Fifteenth*, yet not exceeding a *Two*
and twentieth, than two *Eights* is to be added to the les-
 ser Term, *i. e.* it must be multiplied by four: &c.

[14.] See the division of AB into 3: An. 10. Arithme-
 tically thus: $\frac{1}{3} - \frac{1}{3} = \frac{1}{3}$ X

[15.] *Viz.* for the graver Term. See the division of AB into 4. An. 10.

[16.] For $\frac{1}{2} + \frac{1}{2} = 1$.

[17.] *Viz.* p. 9. And may be made out from the division of AB into six An. 10, if according to the method of our Authour, p. 17, wee convert one halfe thereof, *viz.* from 6 to 3 (which containeth the space of an Eighth) into the Circle following; so that the point at 6 be joynd to the point at 3, and the Circle be divided into three equally (as is 6, 3) at 4 and 5.



[18.] $As \frac{1}{2} - \frac{1}{4} = \frac{1}{4} X.$

[19.] Or composed of one, or more *Eights* only, or together with some one that is contained therein. p. 11.

[20.] $As,$ in Fig. 1, An. 8, is the *Eighth* on the *Chorde* B o; viz. o 21 at 8.

[21.] $As,$ on the same *Chorde*, is 8 21 at 14.

[22.] $As,$ on the same *Chorde*, is 14 21 at 17.

[23.] It should have been only the *Semitone major*; for the *Semitone minor* is not to be found without an other Subdivision.

[24.] *Viz.* An *Eighth*; from the first division of AB, p. 14: a *Fifth*; from the Second; and a *Ditone* from the Third.

[25.] 2 gives the *Eight*; 3 the *Fifth*; and 5 the *Third major*: see also A B An. 10.

[26.] Here endeth the *Former Treat*, as it's called, p. 27; l. 25.

[27.] Whereof p. 55.

[28.] By *Numbers*; as in the first Fig. 10. by *Division*; as of the line A B, p. 14.

[29.] *Viz.* the *Eighth*, *Fifth*, and *Ditone* as before.

[30.] *Viz.* p. 11.

[31.] For both the compounded *Ditones*, as well as the simple, are to be found on a *Chorde* understood to consist

list of but five equall parts; whereas the first compound *Fourth* requireth 8, and the *Second* 16; as in the *Second Fig.* p. 13.

[32.] Proportion is called *Multiplex*; when the greater *Terme* containeth the lesser exactly twice, or oftner: *Superparticular*; when the greater containeth the lesser once, and one certain part thereof: and *Multiplex-superparticular*; when the greater doth containe the lesser twice or oftner, and (besides) one certain part thereof.

[33.] For, as an *Eighth*, divided equally into two parts, doth constitute properly a *Fifth*, and by accident a *Fourth*; so that *Fifth* divided into two equall parts, constituteth properly a *Ditone*, and by accident a *Third minor*: see AB *Animad.* 10.

[34.] For a *Ditone* + *Fourth* = *Sixth major*; a *Ditone* + an *Eighth* = *Tenth major*; and a *Ditone* + *Fifteenth* = *Seventeenth major*. See *Fig.* 1, p. 10, at Numbers 4 and 5; and the division of AB into 5 *Fig.* An. 10.

[35.] For a *Third minor* + a *Fourth* = *Sixth minor*.

$$\frac{2}{3} + \frac{1}{4} = \frac{11}{12}$$

[36.] *Viz.* of the *Graver Term*. See *Fig.* AB An. 10.

[37.] Note, that in every *Musical System*, (whereof there are two sorts; the greater of Ten paralell Lines, and the lesser of Five:) every Line is the seat of one Note, and every intervall of another, and therefore C is a Note higher than B, and G lower than E. See p. 40.

38. For

[38.] For $\frac{1}{2} - \frac{1}{3} = \frac{1}{6}$ i. e. $\frac{1}{12}$ of the Graver Term.

[39.] *Viz.* p.14, where CB, the space of an Eight, is divided into CE a Ditone; ED a Third *minor*; and DB a Fourth.

[40.] *Viz.* by dividing CE p.14, equally into Two, at F: or DG, Fig. An.10. at F: or 14 21 of the Chorde B^o, Fig.1, An.8, at 17.

[41.] By dividing EG, Fig. An.10, at F: or 8 14 of the Chorde B^o, Fig.1, An.8, at 11.

[42.] By dividing GI, Fig. An.10, at H; or EH at G: or 8 of the Chord B^o, Fig.1, An.8, at 6.

[43.] As 6, Fig. 1, An.8, at 2.

[44.] As DG = DE, + EF, + FG; Fig. An. 10: or 14 21, = 14 15, + 15 17, + 17 21; of the Chorde B^o Fig.1, An.8.

[45.] As DE, + EF = DF; Fig. An.10: or 14 15, + 15 17, = 14 17; of the Chorde B^o Fig.1, An.8.

[46.] As 14 15, with 11 14; of the Chorde B^o Fig.1, An.8.

[47.] 64.75 :: 324.379.6875 :: 6'000.7'031.
 $\frac{1}{2} + \frac{1}{3} = \frac{5}{6}$. See Fig.1, An.8.

[48.] Because a *Semitone majus* makes no *Consonance* with the other two.

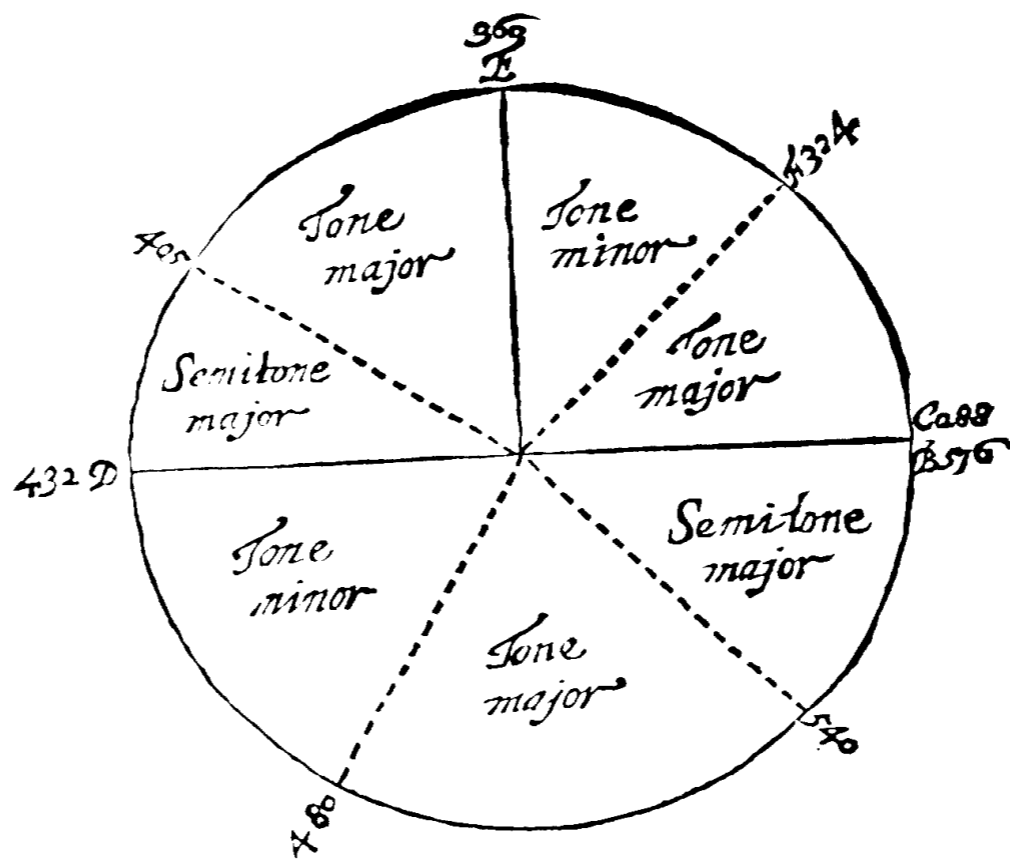
K

[49.] Be-

[49.] Because a *Tone major* maketh a *Third*, with either.

[50.] *Viz.* p.27.

[51.] For otherwise a *major Semitone*, and *minor Tone* must fall together, as may be seene in this following Figure; where the space of an Eighth is turned into a Circle, and divided first, as was CB p. 14, at D and E; and then subdivided as p.27.



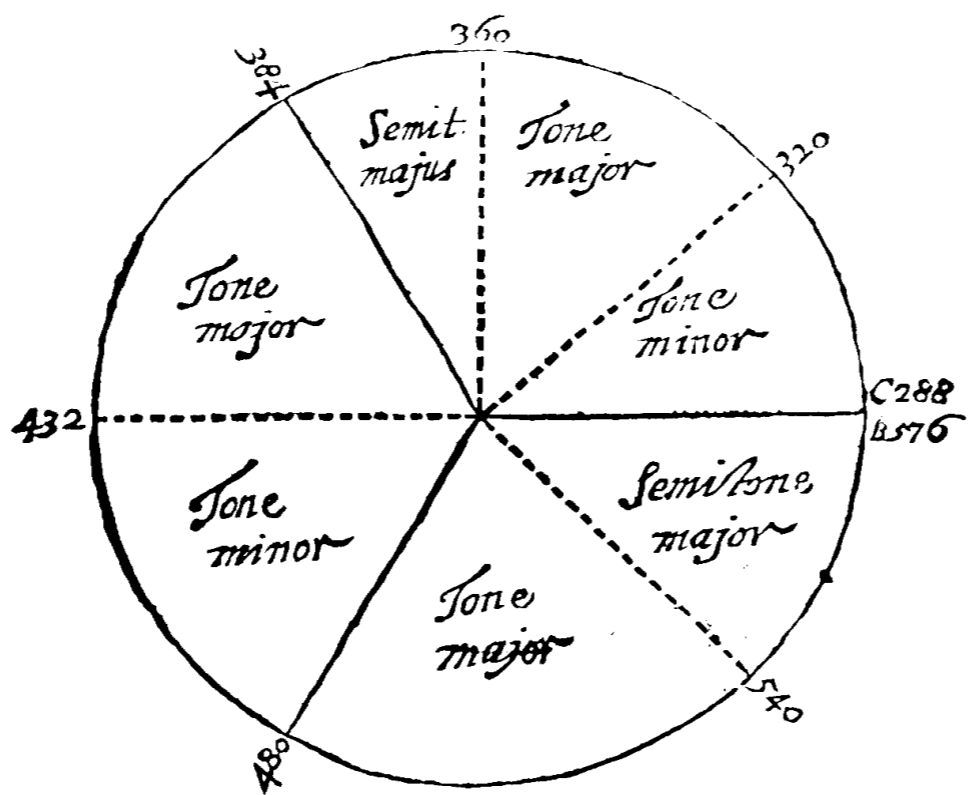
[52.] Others do call it a *Comma major*, See Fig. 1, An. 8.

[53.] And is called *Semitonium medium*, as Fig. 1, An. 8.

[54.] Or

[54.] Or rather 576; because it is the *Gravest Term*, in this instance: as also according to the division of an Eighth, p.14, and 27. See Fig. An.51.

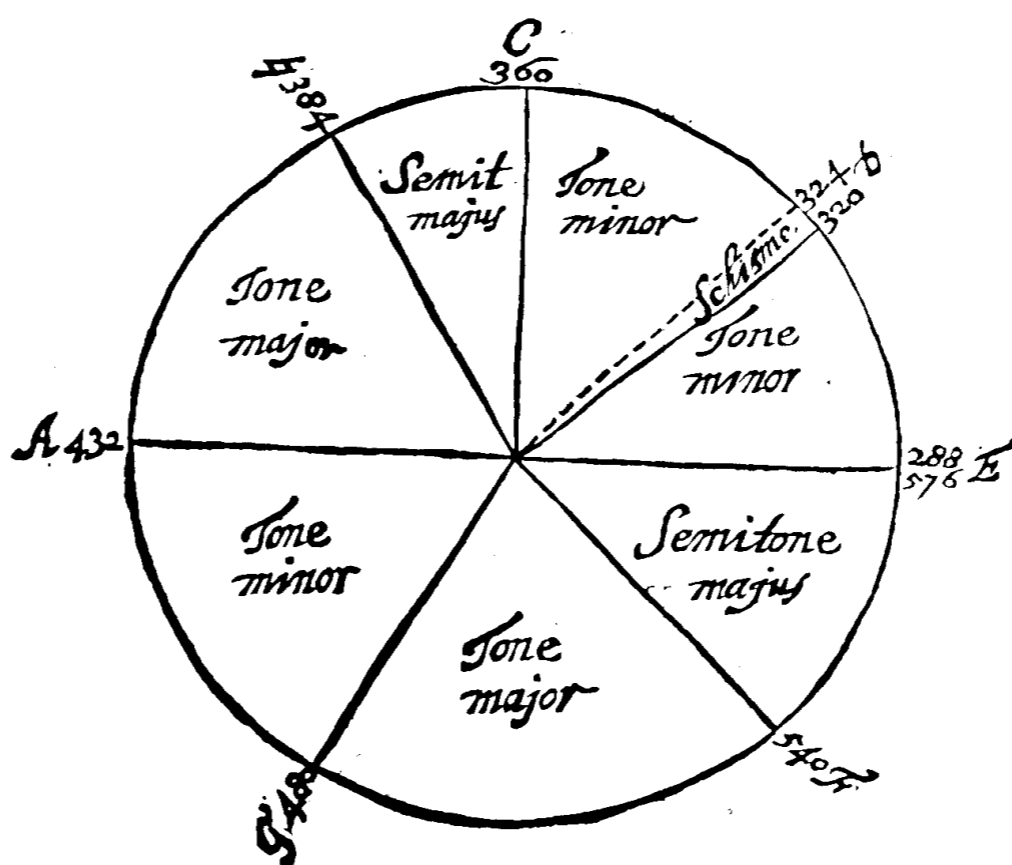
Note that an *Eighth*, divided first into three equal parts, by the division of the whole string into six, as p. 13; and those three then subdivided, as p.28; doth give the Degrees in the same Order: as is to be seen by the following Figure, compared with the former An. 51; this only beginning a *Fourth* from the other, or the other a *Fifth* from this.



K 2

[55.] Only

[55.] Only it seemeth as moved upon its *Center*, till the *Schisme* cometh to be between 324 and 320, as this Figure doth demonstrate, which differeth not from the last (An. 54): only in this the *Schisme* doth stand divided from the *major Tone* (the Intervall between 320, and 360) in that other.



[56.] Here

[56.] Here the Authour recedeth from his former division of an *Eighth*, onely by removing the *Graver Terme* from E to F : as is to bee seen by these two spaces of an

<i>The first</i>				<i>The second</i>			
288	360	432	576	288	360	480	576
270	337.5	405	540	270	360	450	540

Eighth. The first divided as CB, p.14, at D and E: the Second as CI, Fig. An.10, at DG, with both which this doth accord ; E, not F, being made the *Gravest Terme*.

[57.] For from F (the *First Terme* of the *Voice in b flat* ascending) to C (the first in the *Voice Naturall*) is a Fifth; as also from hence to G, where the *Voice in p Sharp* be-
ginneth.

[58.] For p (B Sharpe) is a *Tritone* more Acute than ∇ (F being so accounted) : and a *false, or Semi-Fifth* ∇ than the Δ . But placing the *Graver Terme* at E; then is p; a Fifth more Acute than the *Graver Terme*; and a Fourth more Grave than the *Acuter Terme* : and b flat a *Semi-Fifth* Δ than ∇ ; and a *Tritone* ∇ than Δ . See Fig. p.35.

[59.] *Viz.* p.34. For) is F: [] is C: and G is G.

[60.] *Viz.* Muscally spaces, *i.e.* to every *Tone* the greater, and to every *Semitone* the lesser Intervall.

[61.] As appeareth by this Figure following.

Third major	Third minor	Third major	Third minor	Third major	Third minor	Third major	Third minor
mi. ma.	mi.	ma.	mi.	ma.	mi.	ma.	mi.
Fourth	Tritone	Fourth	Fourth	Fourth	Fourth	Fourth	Fourth
Fifth	Fifth	Fifth	Fifth	Fifth	Fifth	Fifth	Fifth
Sixth major	Sixth minor	Sixth major	Sixth minor	Sixth major	Sixth minor	Sixth major	Sixth minor
Seventh major	Seventh minor	Seventh major	Seventh minor	Seventh major	Seventh minor	Seventh major	Seventh minor
Eighth major	Eighth minor	Eighth major	Eighth minor	Eighth major	Eighth minor	Eighth major	Eighth minor
Ninth major	Ninth minor	Ninth major	Ninth minor	Ninth major	Ninth minor	Ninth major	Ninth minor

[62.] *Viz.* $\frac{1}{12}$ *Semitonium medium*, as before An. 53.

[63.] For $\frac{1}{2} + \frac{1}{3} = \frac{5}{6}$; $\frac{1}{3} + \frac{1}{6} = \frac{1}{2}$; $\frac{1}{6} + \frac{1}{6} = \frac{1}{3}$; $\frac{1}{4} - \frac{1}{6} = \frac{1}{12}$; $\frac{1}{4} - \frac{1}{3} = -\frac{1}{12}$

[64.] See p. 22.

[65.] *Viz.* p. 28.

[66.] See Figure An. 61.

[67.] For $\frac{1}{2} - \frac{1}{3} = \frac{1}{6}$; $\frac{1}{3} - \frac{1}{4} = \frac{1}{12}$; $\frac{1}{4} + \frac{1}{3} = \frac{7}{12}$; $\frac{1}{4} + \frac{1}{6} = \frac{2}{3}$; $\frac{1}{3} + \frac{1}{6} = \frac{1}{2}$

[68.] 480.

		Ninth major	Ninth maxim	Ninth minor
	Seventh minor	Seventh minim		
Sixth minor			Tone ma. mi. Sem. ma. Tone ma. mi. ma. ma. Sem. ma. Tone ma. mi. ma. ma. Sem. ma.	
			Tone ma. mi. Sem. ma. Tone ma. mi. ma. ma. Sem. ma.	
Tone ma. mi. Sem. ma. Tone ma. mi. ma. ma. Sem. ma.				

[68.] $480.405 :: 384.324 :: 32.27.$
 $480.324 :: 40.27.$
 $324.240 :: 27.20.$
 $405.240 :: 324.192 :: 27.16.$

[69.] For $\frac{1}{2} + \frac{12}{135} = \frac{32}{45} : \frac{1}{3} - \frac{12}{135} = \frac{8}{45}.$

[70.] $540.384 :: 405.288 :: 45.32.$
 $384.270 :: 288.202.5 :: 576.405 :: 64.45.$

[71.] viz. the first compound Eighth, i. e. a Fifteenth.

[72.] viz. without altering the order of Succession, p. 30, and 41.

Otherwise, of Eighths considered only as consisting of three major Tones, two minor Tones, and two major Semitones;

mitones ; there are 210 severall sorts, or *Moods* ; and may be found, by the *Laws of Combination*, as in this *Table* following ; where note *a* is put for a *major Tone* ; *b* for a *minor Tone*, and *c* for a *major Semitone*.

a	a	a	b	b	c	c				c	a	b	b	
				c	b	c				b	a	b	a	30
			c	b	b	c		b	a	a	b	c	c	
				c	b	b				c	c	b	c	
		b	a	b	c	c			b	a	c	c	c	
			c	b	c				c	a	c	c	c	
			b	a	c	c	10		c	a	b	c	a	
			c	a	c					b	a	c	b	
			c	a	b	c			b	a	a	c	c	40
			b	a	c	a				c	a	b	a	
				c	a	b			b	a	a	c	c	
		c	a	b	b	c	20		c	a	a	c	a	
			c	b	b					c	a	a	a	
		b	a	b	c	b			c	a	a	b	c	50
			b	a	c					b	a	c	b	
			c	a	b					c	a	a	b	
			c	a	b					b	a	a	b	
				c	a	b				c	a	b	a	

		b	a	a	c					b	a	a	b	a		
			c	c	a					a	a	a	b	a		
		c	a	a	b					b	a	a	c	a	90	
			b	a	a	60				c	b	c	c	b		
c	a	a	b	b	c					b	a	c	c	c		
		b	a	b	c					c	a	c	c	a		
			b	a	c						b	a	c	c		
			c	a	b					c	a	b	c	a		
			c	a	b					b	a	c	a	b	100	
		c	a	b	b	70				c	a	b	a	c		
		b	a	a	b					b	a	a	c	c		
			b	a	b					c	a	c	a	c		
			b	a	c						c	a	a	c		
			c	a	b					c	a	a	b	c		
		b	a	a	c						b	a	c	b	110	
			c	a	a	80				c	a	a	b	c		
			c	a	a					b	a	a	c	a		
			b	a	a						c	a	a	a		
		c	a	b	b					c	a	a	b			

L

			b	a	c					c	a	a	a	b	
				c	a							b	a	a	
				c	a	b						b	a	a	200
		b	a	a	c			c	a	a	a	b	b		
			c	a	a						b	a	b		
			c	a	a							b	a	b	
			c	a	a	b	190			b	a	a	b		
			b	a	a							b	a	a	
	b	a	a	a	c				b	a	a	a	b		
			c	a	a							b	a	a	
			c	a	a							b	a	a	
			c	a	a					b	a	a	a	210	

After the same Method, there are found twelve Fifths, and six Fourths, as followeth.

Fifths

a	a	b	c	1	b	a	a	c	7
		c	b				c	a	
		b	a	c			c	a	a
		c	a		c	a	a	b	
		c	a	b			b	a	
		b	a	6	b	a	a	12	

Fourths

a	b	c	1
	c	b	2
b	a	c	3
	c	a	4
c	a	b	5
	b	a	6

And therefore of Eighths divided into Fourths and Fifths, there are seventy and two severall Moods: and thus of Fifths, divided into Thirds, there are eight Species: &c.

[73.] Viz. both Arithmetically, as 2 3 4, the Fifth before

fore the Fourth ; and *Harmonically*, as 3 4 6, the Fourth before the Fifth, ascending.

[74.] *Viz.* from B to B, *Arithmetically*; and from E to E, *Harmonically*, in b flat : or from F to F, *Arithmetically*; and from B to B, *Harmonically*, in \sharp (B. sharp) p. 41.

[75.] *Viz.* from E to E, in b flat; or from B to B, in \sharp . p. 41.

[76.] *Viz.* from F to F, A to AB, to B, and E to E, in b flat ; or from C to C, E to E, F to F, and B to B, in \sharp . p. 41.

[77.] *Viz.* the two Extreams, and the middle Term.

[78.] See p. 18 and 30.

§ 1. Now considering (as was sayd An. 1 and 3) that not the *visible* proportion of *Chords* or *Strings*, but the *audible* proportion of their *Sounds* only is considerable in Musick ; and that, by the *Sence* of *Hearing*, wee doe judge of *Sounds* according to the *Geometricall*, not *Arithmetical* Proportion, or proportionall *Division* of the *Strings*, that give them : I conceive it was rightly inferred An. 3, that *Chordes*, as to *Sounds*, ought to be divided according to a *Geometricall*, not *Arithmetical* *Progression* ; by force of the same *Reason* (adequated to the *Sence* of *Hearing*) which our *Author* gave for the contrary opinion in his sixth *Preconsiderable*. It therefore remaineth that I heere shew what *Division* it is I mean, and how it may be performed.

§ 2. First then let the Chord AZ, Fig. 2, An. 8, be divided at S, into *Extream* and *Mean Ratio*; by 30.6. *Elem. Euclid.* or by *Prob. 1, c. 19, Clavis Mathematica*; which done, let AS, the *Mean Proportionall*, be divided into 17 *equall Semitones*, by 16 *mean Proportionals*; by the *Latter Table*
of

of Potestates Chap. 12. of Mr. Oughtreds-Clavis Mathem.
 or rather (the other way, in this case, being very labori-
 ous) Chap. 17. Arithmetica Logarithmica H. Briggij.

§ 3. I perform'd it thus.

$AZ = B$
 $AS = A$
 Therefore $ZS = B - A$
 $B - A. A :: A. B.$
 $Aq = Bq - BA$
 $Aq + BA = Bq$
 $Aq + BA + \frac{1}{4}Bq = Bq + \frac{1}{4}Bq$
 $A + \frac{1}{2}B = \sqrt{Bq + \frac{1}{4}Bq}$
 $A = \sqrt{Bq + \frac{1}{4}Bq} - \frac{1}{2}B$
 $B = 10$
 $Bq = 100$
 $\frac{1}{4}Bq = 25$
 $Bq + \frac{1}{4}Bq = 125$
 $\sqrt{Bq + \frac{1}{4}Bq} = 11.18033,98875 -$
 $\frac{1}{2}B = 5$
 $A = 6.18033,98875 -$
 $B - A = 3.81966,01125 +$
 $B = 10.0000,00000 \quad \bar{2} \quad 1,00000,00000$
 $B - A = 3.81966,01125 \quad \bar{2} \quad 0,58202,47162$
 $X \quad 0,41797,52838$
 $\bar{1} \quad 17$
 $\bar{1} \quad 0,02458,67814 = R \quad 1.058 +$
 $\bar{2} \quad B - A \quad 0,58202,47162 = ZS \quad 3.820 -$
 $\bar{1} \quad + ZS \quad 0,60661,14976 \quad ZR \quad 4.042 +$
 $ZR \quad 0,63119,82790 \quad ZQ \quad 4.278 -$
 $ZQ \quad 0,65578,50604 \quad ZP \quad 4.527 -$
 $ZP \quad 0,68037,18418 \quad ZO \quad 4.790 +$
 $L \quad 3 \quad \bar{1} \quad + ZO$

Ad hanc utrum fuerit aptus 16e

☐ + ZO	0,70495,86232	ZN	5'069+
ZN	0,72954,54046	ZM	5'265-
ZM	0,75413,21860	ZL	5'677+
ZL	0,77871,89674	ZK	6'008-
ZK	0,80330,57488	ZI	6'358-
ZI	0,82789,25302	ZH	6'728+
ZH	0,85247,93116	ZG	7'120-
ZG	0,87706,60930	ZF	7'535-
ZF	0,90165,28744	ZE	7'974-
ZE	0,92623,96558	ZD	8'438+
ZD	0,95082,64372	ZC	8'929+
ZC	0,97541,32186	ZB	9'450-
ZB	1,00000,00000	ZA	10'000

§ 4. Into *Extreame and meane Ratio*; that the parts and whole may be \therefore . ZS. SA : : SA. ZA.

§ 5. Into *Seventeen equall Semitones*; because (the Ear not well distinguishing smaller Intervalls) this Number doth best admit of the subsequent *Divisions*, proportionall to their *Extreames*; whence the *Consonances* doe naturally arise, according to this *Analogy*, viz. As the number of parts in the *First Terme*, is to the number of parts in the *Third*; so the number of *Rations* between the *First and Second*, to the number of *Rations* between the *Second and Third*. And may be work'd by either of the following *Rules*.

In Naturall Numbers.

First Rule. $\triangle \text{nr} \sqrt{[\frac{\triangle}{\nabla}]} \text{ } \text{ } [\triangle] \text{ } \text{ } \text{R} = \text{Second Terme.}$

Second Rule. $\nabla \text{nr} \sqrt{[\frac{\triangle}{\nabla}]} \text{ } \text{ } [\nabla] \text{ } \text{ } \text{R} = \text{Second Terme.}$

In Artificiall Numbers, or Logarithmes.

First Rule. $b + \frac{aB - bB}{A + B} = \text{Second Terme.}$

Second Rule. $a - \frac{aA - bA}{A + B} = \text{Second Terme.}$

Note $\frac{\Delta}{\nabla} = \nabla + \Delta : A = \nabla : a = \frac{1}{\Delta} \nabla : B = \Delta : b = \frac{1}{\Delta} \Delta$

5 6. For, from this Division, of the Intervall of an *Eleventh* (i.e. the Meane Proportionall AS); ariseth an *Eighth*, and a *Fourth*: of an *Eighth*; a *Sixth minor*, and a *Third major*: and of a *Sixth minor*; a *Third minor*, and a *Fourth*, and these compounded give the rest.



ZS. ZA:: 5 Semit. 12. fere.

ZN. ZA:: 4. 8. fere.

ZI. ZA:: 3. 5. fere.

Third minor = 3 Semitones.

Third

Third major = 4 Semitones.

Fourth = 5.

Fifth = 7.

Sixth minor = 8.

Sixth major = 9.

Eighth = 12.

This Proportion or Progression, from its excellency and composition, I call Ratio-harmonicall.

§ 7. It may be objected that the R of ZS to ZA is $2 \cdot 61803398875 -$, that is as 5 to 13 +; and therefore SA ought rather to have been divided into 18 proportionall parts, by 17 Meane Proportionalls: whereof 5 = Intervall of a Fourth; and 13 = Space of an Eighth.

§ 8. To which I answer, that SA is understood to be divided into $13 \cdot 8196601125 +$ Proportionall parts: (because the R of ZS to ZA, viz. $2 \cdot 61803398875 -$, is as $3 \cdot 81966,01125 +$ to $10 \cdot 00000,00000$.) whereof the space of an Eighth containeth $10 \cdot 00000,00000$; and of a Fourth $3 \cdot 81966,01125 +$. &c. And may be easily found (by Logarithmes) working, according to the Second Rule, Par. Fifth, thus.

$$AZ = 10 \cdot 00000,00000 \quad \bar{z} \quad 1,00000,00000.$$

$$ZS = 3 \cdot 81966,01125 \quad \bar{z} \quad 0,58202,47162.$$

$$\underline{0,41797,52838,00000000000.}$$

$$13 \cdot 8196601125$$

$$\underline{0,3024497566.}$$

$$0,69755,02434 = ZN, 4 \cdot 98368,11082.$$

$$AZ = 10 \cdot 00000,00000 \quad \bar{z} \quad 1,00000,00000.$$

$$ZN = 4 \cdot 98368,11082 \quad \bar{z} \quad 0,69755,02434.$$

$$\underline{0,30244,97566,00000000000.}$$

$$14 \cdot 9836811082$$

$$\underline{0,20185,27720.}$$

$$0,7981472280 = ZI, 6 \cdot 28271,31146$$

ZA

$$\begin{aligned}
 ZA &= 10^{\cdot}00000,00000 \sqrt[17]{1,00000,00000.} \\
 ZI &= 6^{\cdot}28271,31146 \sqrt[17]{0,79814,72280.} \\
 & \quad 0,20185,27720,00000000000. \\
 & \quad 10^{\cdot}2827131146 \\
 & \quad 0,12396,75296. \\
 & \quad 0,87603,24704. = ZF.7^{\cdot}51679,09301
 \end{aligned}$$

s. 9. But this exactnesse is not requisite, since the *Sense of Hearing* is not so perfect, as to confine the *Consonances* to so precise a *Measure*; (see p. 46.) and therefore, seeing that SA divided into 17 Proportionall Spaces, doth give (without any *Fraction*, or sensible difference,) all the simple *Consonances*; & that $\frac{3^{\cdot}1966^{\cdot}4}{100^{\cdot}0000} = \frac{4^{\cdot}7745^{\cdot}4}{12^{\cdot}5000}$ that is, without *Fraction*, $\frac{1}{12}$; as because, if SA be divided into 18 Proportionall *Intervalls*, NA (containing 13 of them) cannot be divided at I without a *Fraction*, much lesse again at F, I made 17 Par. 3. with which the common *Division* doth not ill accord; for so many *Semitones* are contained in an *Eleventh*.

s. 10. Thus then having resolved that the *Proportion* of ZS to ZA is, as to the practick, exactly enough accounted as 5 to 12: It must follow, by force of the preceding Rules Par. 5. that (1) the *Product* of $3^{\cdot}1966,01125$ Multiplied by the Seventeenth *Root* of the Fifth *Potestas* of $2^{\cdot}61803398875$; or (2) the *Quotient* of $10^{\cdot}00000,00000$ Divided by the Seventeenth *Root* of the Twelfth *Potestas*, of $2^{\cdot}61803398875 = ZN$. And by *Logarithmes* as followeth.

M ZA

AZ =	10'00000,00000	Σ	1,00000,00000	
ZN =	3'81966,01125	Σ	0,58202,47162	
		X	0,41797,52838	0,41797,52838
		m ^r	5	18
		n ^r	2 08987,64190	5,01570,34056
		□	17	17
		□	0,12293,39070	0,29504,13768
		Σ Δ	0,58202,47162	▽ 1,00000,00000
		L	0,70495,86232	X 0,70495,86232

the *Logarithme* of (ZN) 5'069+. differing from the former, Par. 8, about the *Intervall* of a *Schisma*, or *Comma*, *majus*, no perceptible *Dissonance*, as p. 33.

§ 11. Then ZN being to ZA, as 1 to 2 *ferè*; therefore, by the Second Rule in *Logarithmes*, Par. 5.

Σ ZA	1,00000,00000	
ZN	0,70495,86232	
	0,29504,13768	2
	0,59008,27536	
	3	
	0,19669,42512	
	1,00000,00000	
	0,80330,57488	Σ ZI, 6'358"

§ 12. Lastly ZI and ZA being as 3 to 5 *ferè*; therefore

Σ ZA	1,00000,00000
ZI	0,80330,57488
	0,19669,42512
	5

0,98347

0,98347,12560
8

0,12293,39070

1,00000,00000

0,87706,60930 2 ZF, 7535 -

§ 13. *With what hath been here said, if the Reader please to be satisfied at present; I shall, when, if ever, I have (God mercifully assisting) laboured through my tedious Troubles and Distractions, endeavour his better compensation with an entire and particular Tract, according to this new Theory. (And hence too shall shew how Astrologers may deduce their Aspects; with more, I presume, of satisfaction, than from any other hitherto discovered to them. And perhaps with somewhat else more worthy the Reader's paines, and mine.) If not; I here further present him the two following Divisions of a Chord, and will so leave him to seeke it there, or where else he pleaseth.*

§ 14. *The One (approved by many Excellent Mathematicians; See Mersennus Lib. I. de Instrumentis Harmonicis, Prop. 15.) is the Division of ZA, Fig. 3, An. 8, first into two equall parts at N; and then of NA into twelve equall Semitones, by eleven Meane Proportionalls, according to this Table following.*

M 2

11

In Species,		Numbers Surde,
ZN	E = Δ. ZN.	5 000
ZM	√ 12 AEcccq.	√cccc 488281250.00c00000000,000 000000 000,00000000000000
ZL	√ 6 AEcq.	√cc 21250 000000,00 0000,000000
ZK	√ 4 AEc.	√qq 1250.0000,0000,0000
ZI	√ 3 AEq.	√c 250.000,000,000
ZH	√ 12 AcqEcq.	√ccc 7812500000.0000000000,000 000000000,0000000000
ZG	√ AE.	√ 50. 00 00,00
ZF	√ 12 AcqqEcq.	√ccc 31250000000.0000000000,00 0000000000,0000000000
ZE	√ 3 AcqE.	√c 500. 000, 000, 000
ZD	√ 4 AcE.	√qq 5000. 0000, 0000, 0000
ZC	√ 6 AcqE.	√cc 50000.000000,000000,000000
ZB	√ 12 AcccqE.	√cccc 500000000000.0000000000,00 0000000000,0000000000
ZA	A = ∇. ZA.	10.000

Logarithmes,		Numb. D.
ZN	0, 69897, 00043.	5'000
ZM	0, 72405, 58372.3	5'297+
ZL	0, 74914, 16702.2	5'632+
ZK	0, 77422, 75032.1	5'946+
ZI	0, 79931, 33362.	6'300-
ZH	0, 82439, 91691.3	6'674+
ZG	0, 84948, 50021.2	7'071+
ZF	0, 87457, 08351.1	7'492-
ZE	0, 89965, 66681.	7'937+
ZD	0, 92474, 25010.3	8'409-
ZC	0, 94982, 83340.2	8'909-
ZB	0, 97491, 41670.1	9'439-
ZA	1, 00000, 00000.	10'000

Musick Compendium of R. Des Cartes.

§ 15. The Order is the Division of ZA, Fig. 4. An. 8, Harmonic at Q, and of QA into 15 equal Semitones.

The manner thus.

ZA = B

ZQ = A

Therefore QA = B - A

A.B :: B - 2A.A.

B = 10.

Aq = Bq - 2BA

Bq = 100.

Bq = Aq + 2BA

2Bq = 200.

2Bq = Aq + 2BA + Bq $\sqrt{2Bq} = \frac{14.1421+}{2}$

$\sqrt{2B} = A + B$

A = $\frac{4.1421+}{2}$

$\sqrt{2Bq} = B = A$

B - A = 5.8579-

B = 10.000 $\frac{3}{4}$ 1,0000,00.

A = $\frac{4.1421+}{2}$ 0,61721,48.

X 0,38277,52.

15:

$\frac{0.02591,87}{15} = R$ 1.661-

$\frac{3}{4} A$ 0,61721,48. = ZQ 4.142+

+ZQ 0,64274,31.7 ZP 4.393-

ZP 0,66826,14.14 ZO 4.659-

ZO 0,69377,98.6 ZN 4.941-

ZN 0,71929,81.13 ZM 5.240-

ZM 0,74481,65.5 ZL 5.557-

ZL 0,77033,48.12 ZK 5.893-

ZK 0,79585,32.4 ZI 6.250-

ZI 0,82137,15.11 ZH 6.628-

ZH 0,84688,99.3 ZG 7.029-

ZG 0,87240,82.10 ZF 7.454+

ZF 0,89792,66.2 ZE 7.905+

ZE 0,92344,49.9 ZD 8.384-

M 3.

← ZD

Animadversions upon the, &c.

+ ZD 0,94896,33.1 ZC 8.891 +
ZC 0,97448,16,8 ZB 0'429 +
ZB 1,00000,00. ZA 10'000

§ 16. And lastly, that the *Reader* may, with the less trouble, compare these severall *Divisions* each with other; I have both reduced our *Authors* Numbers to these, and these to his. See Fig. 1, 2, 3, and 4. An. 6.

FINIS.

These Errors

Amend thus.

P.	L.		
3	16	[5]	[5]
7	24	} Consonancies	Consonances
8	6		
11	25		
12	26		
12	1	} Hexachordon minus, Eight	Hexachordon minus, Eight
17	24		
17	2	} Diapason	Diapason
19	23		
18	30	an Eighth [26].	[26] an Eighth [26].
21	1	o Fi dar	a Fifth, and
22	6	defumed	defumed
23	6	For Example,	than, for Example, betweene
23	7	than betweene	Muficians
25	10	Muficians	Muficians
34	8	Muficians	
44	13	} observed, that a voyce [65] doth	} observed [65], that a voice doth
53	30		
53	19	Synco-p	Synco-p.
54	30	a Eighth.	an Eighth.
55	3	a Vnison.	an Vnison.
65	23	*	▽
69	18	△	△
71	2	* Eights	Eights
71	14	} Eight	Eighth.
73	2	Former Tract,	Superior Tractate,
74	16	Fig. 10.	Fig. p. 10.
75	6	13; and those three then subdivided, as p. 28;	10; and those three then subdivided, as p. 27.
78	7	1	2
84	8	A to AB to B,	A to A, B to B;
85	3	Chap.	Cap.

